

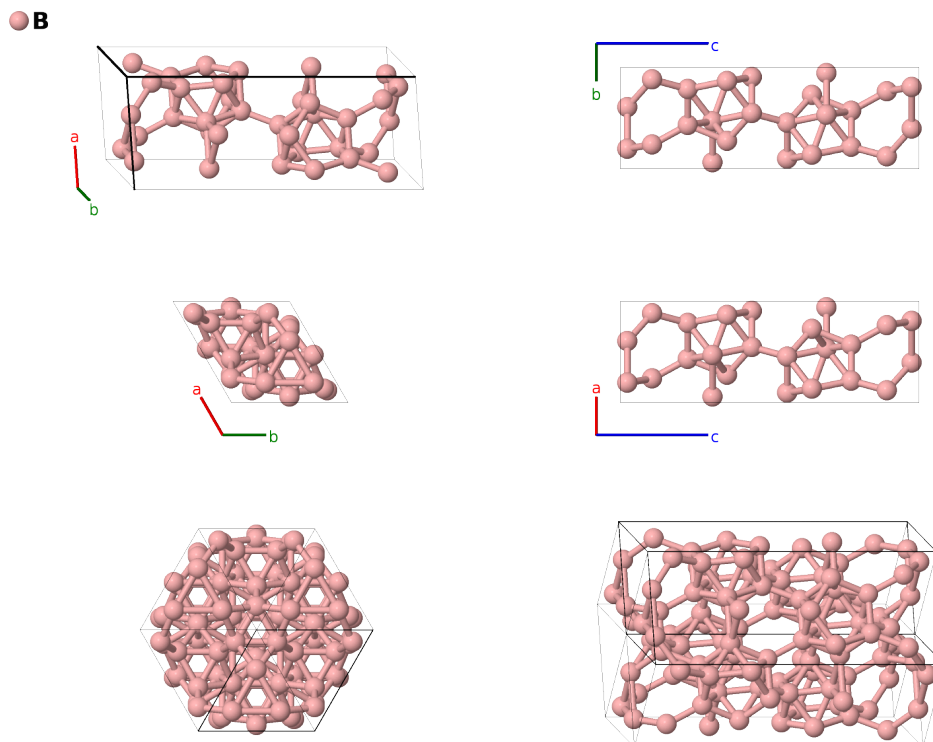
# $\alpha$ -B (R-12) Structure: A\_hR12\_166\_2h-001

This structure originally had the label A\_hR12\_166\_2h. Calls to that address will be redirected here.

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<https://aflow.org/p/1Y2H>

[https://aflow.org/p/A\\_hR12\\_166\\_2h-001](https://aflow.org/p/A_hR12_166_2h-001)



Prototype	B
AFLOW prototype label	A_hR12_166_2h-001
ICSD	26487
Pearson symbol	hR12
Space group number	166
Space group symbol	$R\bar{3}m$
AFLOW prototype command	<code>aflow --proto=A_hR12_166_2h-001 --params=a, c/a, x<sub>1</sub>, z<sub>1</sub>, x<sub>2</sub>, z<sub>2</sub></code>

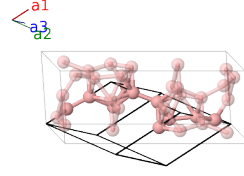
- This is a metastable phase of boron, also known as rhombohedral-12 boron (Donohue, 1982). It is the simplest known phase (the ground state,  $\beta$ -B, has 105 atoms in the primitive cell).
- Note the relationship between the icosahedra in this structure,  $\beta$ -B and T-50 B.

- Hexagonal settings for rhombohedral structures can be obtained with the option `--hex`.

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## Rhombohedral primitive vectors

$$\begin{aligned}\mathbf{a}_1 &= \frac{1}{2}a \hat{\mathbf{x}} - \frac{\sqrt{3}}{6}a \hat{\mathbf{y}} + \frac{1}{3}c \hat{\mathbf{z}} \\ \mathbf{a}_2 &= \frac{1}{\sqrt{3}}a \hat{\mathbf{y}} + \frac{1}{3}c \hat{\mathbf{z}} \\ \mathbf{a}_3 &= -\frac{1}{2}a \hat{\mathbf{x}} - \frac{\sqrt{3}}{6}a \hat{\mathbf{y}} + \frac{1}{3}c \hat{\mathbf{z}}\end{aligned}$$




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## Basis vectors

	Lattice coordinates		Cartesian coordinates	Wyckoff position	Atom type
$\mathbf{B}_1$	$x_1 \mathbf{a}_1 + x_1 \mathbf{a}_2 + z_1 \mathbf{a}_3$	=	$\frac{1}{2}a(x_1 - z_1) \hat{\mathbf{x}} + \frac{\sqrt{3}}{6}a(x_1 - z_1) \hat{\mathbf{y}} + \frac{1}{3}c(2x_1 + z_1) \hat{\mathbf{z}}$	(6h)	B I
$\mathbf{B}_2$	$z_1 \mathbf{a}_1 + x_1 \mathbf{a}_2 + x_1 \mathbf{a}_3$	=	$-\frac{1}{2}a(x_1 - z_1) \hat{\mathbf{x}} + \frac{\sqrt{3}}{6}a(x_1 - z_1) \hat{\mathbf{y}} + \frac{1}{3}c(2x_1 + z_1) \hat{\mathbf{z}}$	(6h)	B I
$\mathbf{B}_3$	$x_1 \mathbf{a}_1 + z_1 \mathbf{a}_2 + x_1 \mathbf{a}_3$	=	$-\frac{1}{\sqrt{3}}a(x_1 - z_1) \hat{\mathbf{y}} + \frac{1}{3}c(2x_1 + z_1) \hat{\mathbf{z}}$	(6h)	B I
$\mathbf{B}_4$	$-z_1 \mathbf{a}_1 - x_1 \mathbf{a}_2 - x_1 \mathbf{a}_3$	=	$\frac{1}{2}a(x_1 - z_1) \hat{\mathbf{x}} - \frac{\sqrt{3}}{6}a(x_1 - z_1) \hat{\mathbf{y}} - \frac{1}{3}c(2x_1 + z_1) \hat{\mathbf{z}}$	(6h)	B I
$\mathbf{B}_5$	$-x_1 \mathbf{a}_1 - x_1 \mathbf{a}_2 - z_1 \mathbf{a}_3$	=	$-\frac{1}{2}a(x_1 - z_1) \hat{\mathbf{x}} - \frac{\sqrt{3}}{6}a(x_1 - z_1) \hat{\mathbf{y}} - \frac{1}{3}c(2x_1 + z_1) \hat{\mathbf{z}}$	(6h)	B I
$\mathbf{B}_6$	$-x_1 \mathbf{a}_1 - z_1 \mathbf{a}_2 - x_1 \mathbf{a}_3$	=	$\frac{1}{\sqrt{3}}a(x_1 - z_1) \hat{\mathbf{y}} - \frac{1}{3}c(2x_1 + z_1) \hat{\mathbf{z}}$	(6h)	B I
$\mathbf{B}_7$	$x_2 \mathbf{a}_1 + x_2 \mathbf{a}_2 + z_2 \mathbf{a}_3$	=	$\frac{1}{2}a(x_2 - z_2) \hat{\mathbf{x}} + \frac{\sqrt{3}}{6}a(x_2 - z_2) \hat{\mathbf{y}} + \frac{1}{3}c(2x_2 + z_2) \hat{\mathbf{z}}$	(6h)	B II
$\mathbf{B}_8$	$z_2 \mathbf{a}_1 + x_2 \mathbf{a}_2 + x_2 \mathbf{a}_3$	=	$-\frac{1}{2}a(x_2 - z_2) \hat{\mathbf{x}} + \frac{\sqrt{3}}{6}a(x_2 - z_2) \hat{\mathbf{y}} + \frac{1}{3}c(2x_2 + z_2) \hat{\mathbf{z}}$	(6h)	B II
$\mathbf{B}_9$	$x_2 \mathbf{a}_1 + z_2 \mathbf{a}_2 + x_2 \mathbf{a}_3$	=	$-\frac{1}{\sqrt{3}}a(x_2 - z_2) \hat{\mathbf{y}} + \frac{1}{3}c(2x_2 + z_2) \hat{\mathbf{z}}$	(6h)	B II
$\mathbf{B}_{10}$	$-z_2 \mathbf{a}_1 - x_2 \mathbf{a}_2 - x_2 \mathbf{a}_3$	=	$\frac{1}{2}a(x_2 - z_2) \hat{\mathbf{x}} - \frac{\sqrt{3}}{6}a(x_2 - z_2) \hat{\mathbf{y}} - \frac{1}{3}c(2x_2 + z_2) \hat{\mathbf{z}}$	(6h)	B II
$\mathbf{B}_{11}$	$-x_2 \mathbf{a}_1 - x_2 \mathbf{a}_2 - z_2 \mathbf{a}_3$	=	$-\frac{1}{2}a(x_2 - z_2) \hat{\mathbf{x}} - \frac{\sqrt{3}}{6}a(x_2 - z_2) \hat{\mathbf{y}} - \frac{1}{3}c(2x_2 + z_2) \hat{\mathbf{z}}$	(6h)	B II
$\mathbf{B}_{12}$	$-x_2 \mathbf{a}_1 - z_2 \mathbf{a}_2 - x_2 \mathbf{a}_3$	=	$\frac{1}{\sqrt{3}}a(x_2 - z_2) \hat{\mathbf{y}} - \frac{1}{3}c(2x_2 + z_2) \hat{\mathbf{z}}$	(6h)	B II

## References

- [1] B. F. Decker and J. S. Kasper, *The crystal structure of a simple rhombohedral form of boron*, Acta Cryst. **12**, 503–506 (1959), doi:10.1107/S0365110X59001529.

## Found in

- [1] J. Donohue, *The Structures of the Elements* (Robert E. Krieger Publishing Company, New York, 1974).