

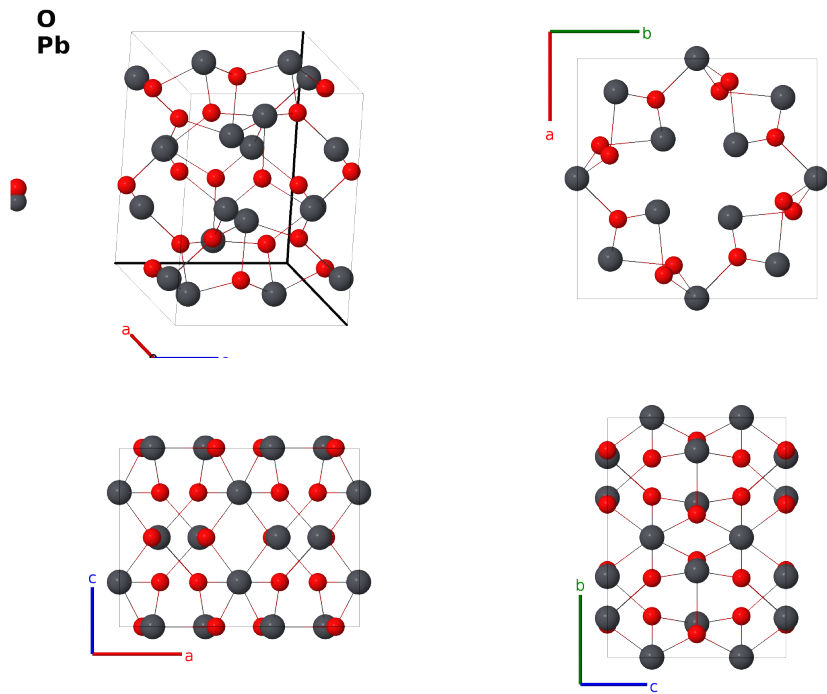
Minium-T (Pb_3O_4) Structure: A4B3_tP28_135_gh_dh-002

Cite this page as:

- H. Eckert, S. Divilov, M. J. Mehl, D. Hicks, A. C. Zettel, M. Esters, X. Campilongo, and S. Curtarolo, *The AFLOW Library of Crystallographic Prototypes: Part 4*, Comput. Mater. Sci. **240**, 112988 (2024), doi: 10.1016/j.commatsci.2024.112988.
- D. Hicks, M. J. Mehl, M. Esters, C. Oses, O. Levy, G. L. W. Hart, C. Toher, and S. Curtarolo, *The AFLOW Library of Crystallographic Prototypes: Part 3*, Comput. Mater. Sci. **199**, 110450 (2021), doi: 10.1016/j.commatsci.2021.110450.

<https://aflow.org/prototype-encyclopedia/68YC>

https://aflow.org/prototype-encyclopedia/A4B3_tP28_135_gh_dh-002



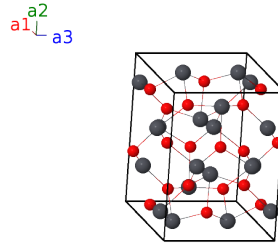
Prototype	O_4Pb_3
AFLOW prototype label	A4B3_tP28_135_gh_dh-002
Mineral name	minium
ICSD	4106
CCDC	1592812
Pearson symbol	tP28
Space group number	135
Space group symbol	$P4_2/mbc$
AFLOW prototype command	<code>aflow --proto=A4B3_tP28_135_gh_dh-002</code> <code>--params=a, c/a, x₂, x₃, y₃, x₄, y₄</code>

- Pb_3O_4 has been observed in several structures (Wriedt, 1988; Dinnebier, 2003):

- Below 170K (Wriedt, 1988) it is in the orthorhombic Minium-R structure. (Gavarri, 1978) tracks this structure up to 240K.
- Above 170K it is in the tetragonal Minium-T structure (this structure).
- At ambient temperature the Minium-T structure transforms into what is apparently the Minium-R structure at a pressure between 0.11 and 0.3 GPa. (Dinnebier, 2003) call this *Phase II*.
- If the pressure is increased, between 5.54 and 6.6 GPa the structure transforms into orthorhombic Phase III structure.
- The first determination of this structure was made by (Gross, 1943), who assigned it to space group $P\bar{4}b2$ #117 (ICSD 29094, AFLOW label A4B3_tP28_135_gh_dh-001), but that structure is practically indistinguishable from the current structure.
- We assign tenary compounds related to this structure to prototype ZnSb_2O_4 .

Simple Tetragonal primitive vectors

$$\begin{aligned} \mathbf{a}_1 &= a \hat{\mathbf{x}} \\ \mathbf{a}_2 &= a \hat{\mathbf{y}} \\ \mathbf{a}_3 &= c \hat{\mathbf{z}} \end{aligned}$$



Basis vectors

	Lattice coordinates		Cartesian coordinates	Wyckoff position	Atom type
$\mathbf{B}_1$	$= \frac{1}{2} \mathbf{a}_2 + \frac{1}{4} \mathbf{a}_3$	$=$	$\frac{1}{2}a \hat{\mathbf{y}} + \frac{1}{4}c \hat{\mathbf{z}}$	(4d)	Pb I
$\mathbf{B}_2$	$= \frac{1}{2} \mathbf{a}_1 + \frac{3}{4} \mathbf{a}_3$	$=$	$\frac{1}{2}a \hat{\mathbf{x}} + \frac{3}{4}c \hat{\mathbf{z}}$	(4d)	Pb I
$\mathbf{B}_3$	$= \frac{1}{2} \mathbf{a}_2 + \frac{3}{4} \mathbf{a}_3$	$=$	$\frac{1}{2}a \hat{\mathbf{y}} + \frac{3}{4}c \hat{\mathbf{z}}$	(4d)	Pb I
$\mathbf{B}_4$	$= \frac{1}{2} \mathbf{a}_1 + \frac{1}{4} \mathbf{a}_3$	$=$	$\frac{1}{2}a \hat{\mathbf{x}} + \frac{1}{4}c \hat{\mathbf{z}}$	(4d)	Pb I
$\mathbf{B}_5$	$= x_2 \mathbf{a}_1 + (x_2 + \frac{1}{2}) \mathbf{a}_2 + \frac{1}{4} \mathbf{a}_3$	$=$	$ax_2 \hat{\mathbf{x}} + a(x_2 + \frac{1}{2}) \hat{\mathbf{y}} + \frac{1}{4}c \hat{\mathbf{z}}$	(8g)	O I
$\mathbf{B}_6$	$= -x_2 \mathbf{a}_1 - (x_2 - \frac{1}{2}) \mathbf{a}_2 + \frac{1}{4} \mathbf{a}_3$	$=$	$-ax_2 \hat{\mathbf{x}} - a(x_2 - \frac{1}{2}) \hat{\mathbf{y}} + \frac{1}{4}c \hat{\mathbf{z}}$	(8g)	O I
$\mathbf{B}_7$	$= -(x_2 - \frac{1}{2}) \mathbf{a}_1 + x_2 \mathbf{a}_2 + \frac{3}{4} \mathbf{a}_3$	$=$	$-a(x_2 - \frac{1}{2}) \hat{\mathbf{x}} + ax_2 \hat{\mathbf{y}} + \frac{3}{4}c \hat{\mathbf{z}}$	(8g)	O I
$\mathbf{B}_8$	$= (x_2 + \frac{1}{2}) \mathbf{a}_1 - x_2 \mathbf{a}_2 + \frac{3}{4} \mathbf{a}_3$	$=$	$a(x_2 + \frac{1}{2}) \hat{\mathbf{x}} - ax_2 \hat{\mathbf{y}} + \frac{3}{4}c \hat{\mathbf{z}}$	(8g)	O I
$\mathbf{B}_9$	$= -x_2 \mathbf{a}_1 - (x_2 - \frac{1}{2}) \mathbf{a}_2 + \frac{3}{4} \mathbf{a}_3$	$=$	$-ax_2 \hat{\mathbf{x}} - a(x_2 - \frac{1}{2}) \hat{\mathbf{y}} + \frac{3}{4}c \hat{\mathbf{z}}$	(8g)	O I
$\mathbf{B}_{10}$	$= x_2 \mathbf{a}_1 + (x_2 + \frac{1}{2}) \mathbf{a}_2 + \frac{3}{4} \mathbf{a}_3$	$=$	$ax_2 \hat{\mathbf{x}} + a(x_2 + \frac{1}{2}) \hat{\mathbf{y}} + \frac{3}{4}c \hat{\mathbf{z}}$	(8g)	O I
$\mathbf{B}_{11}$	$= (x_2 + \frac{1}{2}) \mathbf{a}_1 - x_2 \mathbf{a}_2 + \frac{1}{4} \mathbf{a}_3$	$=$	$a(x_2 + \frac{1}{2}) \hat{\mathbf{x}} - ax_2 \hat{\mathbf{y}} + \frac{1}{4}c \hat{\mathbf{z}}$	(8g)	O I
$\mathbf{B}_{12}$	$= -(x_2 - \frac{1}{2}) \mathbf{a}_1 + x_2 \mathbf{a}_2 + \frac{1}{4} \mathbf{a}_3$	$=$	$-a(x_2 - \frac{1}{2}) \hat{\mathbf{x}} + ax_2 \hat{\mathbf{y}} + \frac{1}{4}c \hat{\mathbf{z}}$	(8g)	O I
$\mathbf{B}_{13}$	$= x_3 \mathbf{a}_1 + y_3 \mathbf{a}_2$	$=$	$ax_3 \hat{\mathbf{x}} + ay_3 \hat{\mathbf{y}}$	(8h)	O II
$\mathbf{B}_{14}$	$= -x_3 \mathbf{a}_1 - y_3 \mathbf{a}_2$	$=$	$-ax_3 \hat{\mathbf{x}} - ay_3 \hat{\mathbf{y}}$	(8h)	O II
$\mathbf{B}_{15}$	$= -y_3 \mathbf{a}_1 + x_3 \mathbf{a}_2 + \frac{1}{2} \mathbf{a}_3$	$=$	$-ay_3 \hat{\mathbf{x}} + ax_3 \hat{\mathbf{y}} + \frac{1}{2}c \hat{\mathbf{z}}$	(8h)	O II
$\mathbf{B}_{16}$	$= y_3 \mathbf{a}_1 - x_3 \mathbf{a}_2 + \frac{1}{2} \mathbf{a}_3$	$=$	$ay_3 \hat{\mathbf{x}} - ax_3 \hat{\mathbf{y}} + \frac{1}{2}c \hat{\mathbf{z}}$	(8h)	O II
$\mathbf{B}_{17}$	$= -(x_3 - \frac{1}{2}) \mathbf{a}_1 + (y_3 + \frac{1}{2}) \mathbf{a}_2$	$=$	$-a(x_3 - \frac{1}{2}) \hat{\mathbf{x}} + a(y_3 + \frac{1}{2}) \hat{\mathbf{y}}$	(8h)	O II
$\mathbf{B}_{18}$	$= (x_3 + \frac{1}{2}) \mathbf{a}_1 - (y_3 - \frac{1}{2}) \mathbf{a}_2$	$=$	$a(x_3 + \frac{1}{2}) \hat{\mathbf{x}} - a(y_3 - \frac{1}{2}) \hat{\mathbf{y}}$	(8h)	O II

$$\mathbf{B}_{19} = (y_3 + \frac{1}{2}) \mathbf{a}_1 + (x_3 + \frac{1}{2}) \mathbf{a}_2 + \frac{1}{2} \mathbf{a}_3 = a (y_3 + \frac{1}{2}) \hat{\mathbf{x}} + a (x_3 + \frac{1}{2}) \hat{\mathbf{y}} + \frac{1}{2} c \hat{\mathbf{z}} \quad (8h) \quad \text{O II}$$

$$\mathbf{B}_{20} = - (y_3 - \frac{1}{2}) \mathbf{a}_1 - (x_3 - \frac{1}{2}) \mathbf{a}_2 + \frac{1}{2} \mathbf{a}_3 = -a (y_3 - \frac{1}{2}) \hat{\mathbf{x}} - a (x_3 - \frac{1}{2}) \hat{\mathbf{y}} + \frac{1}{2} c \hat{\mathbf{z}} \quad (8h) \quad \text{O II}$$

$$\mathbf{B}_{21} = x_4 \mathbf{a}_1 + y_4 \mathbf{a}_2 = ax_4 \hat{\mathbf{x}} + ay_4 \hat{\mathbf{y}} \quad (8h) \quad \text{Pb II}$$

$$\mathbf{B}_{22} = -x_4 \mathbf{a}_1 - y_4 \mathbf{a}_2 = -ax_4 \hat{\mathbf{x}} - ay_4 \hat{\mathbf{y}} \quad (8h) \quad \text{Pb II}$$

$$\mathbf{B}_{23} = -y_4 \mathbf{a}_1 + x_4 \mathbf{a}_2 + \frac{1}{2} \mathbf{a}_3 = -ay_4 \hat{\mathbf{x}} + ax_4 \hat{\mathbf{y}} + \frac{1}{2} c \hat{\mathbf{z}} \quad (8h) \quad \text{Pb II}$$

$$\mathbf{B}_{24} = y_4 \mathbf{a}_1 - x_4 \mathbf{a}_2 + \frac{1}{2} \mathbf{a}_3 = ay_4 \hat{\mathbf{x}} - ax_4 \hat{\mathbf{y}} + \frac{1}{2} c \hat{\mathbf{z}} \quad (8h) \quad \text{Pb II}$$

$$\mathbf{B}_{25} = - (x_4 - \frac{1}{2}) \mathbf{a}_1 + (y_4 + \frac{1}{2}) \mathbf{a}_2 = -a (x_4 - \frac{1}{2}) \hat{\mathbf{x}} + a (y_4 + \frac{1}{2}) \hat{\mathbf{y}} \quad (8h) \quad \text{Pb II}$$

$$\mathbf{B}_{26} = (x_4 + \frac{1}{2}) \mathbf{a}_1 - (y_4 - \frac{1}{2}) \mathbf{a}_2 = a (x_4 + \frac{1}{2}) \hat{\mathbf{x}} - a (y_4 - \frac{1}{2}) \hat{\mathbf{y}} \quad (8h) \quad \text{Pb II}$$

$$\mathbf{B}_{27} = (y_4 + \frac{1}{2}) \mathbf{a}_1 + (x_4 + \frac{1}{2}) \mathbf{a}_2 + \frac{1}{2} \mathbf{a}_3 = a (y_4 + \frac{1}{2}) \hat{\mathbf{x}} + a (x_4 + \frac{1}{2}) \hat{\mathbf{y}} + \frac{1}{2} c \hat{\mathbf{z}} \quad (8h) \quad \text{Pb II}$$

$$\mathbf{B}_{28} = - (y_4 - \frac{1}{2}) \mathbf{a}_1 - (x_4 - \frac{1}{2}) \mathbf{a}_2 + \frac{1}{2} \mathbf{a}_3 = -a (y_4 - \frac{1}{2}) \hat{\mathbf{x}} - a (x_4 - \frac{1}{2}) \hat{\mathbf{y}} + \frac{1}{2} c \hat{\mathbf{z}} \quad (8h) \quad \text{Pb II}$$

References

- [1] J. R. Gavarri and D. Weigel, *Oxydes de plomb. I. Structure cristalline du minium Pb_3O_4 , à température ambiante (293 K)*, J. Solid State Chem. **13**, 252–257 (1975), doi:10.1016/0022-4596(75)90127-9.
- [2] R. E. Dinnebier, S. Carlson, M. Hanfland, and M. Jansen, *Bulk moduli and high-pressure crystal structures of minium, Pb_3O_4 , determined by X-ray powder diffraction*, Am. Mineral. **88**, 996–1002 (2003), doi:10.2138/am-2003-0707.
- [3] J. R. Gavarri, D. Weigel, and A. W. Hewat, *Oxydes de plomb. IV. Evolution structurale de l'oxyde Pb_3O_4 entre 240 et 5° K et mécanisme de la transition*, J. Solid State Chem. **23**, 327–339 (1978), doi:10.1016/0022-4596(78)90081-6.
- [4] S. T. Gross, *The Crystal Structure of Pb_3O_4* , J. Am. Chem. Soc. **65**, 1107–1110 (1943), doi:10.1021/ja01246a029.

Found in

- [1] H. A. Wriedt, *The O-Pb (Oxygen-Lead) System*, Bull. Alloy Phase Diag. **9**, 106–127 (1988).

First cited in

N. Anderson, M. J. Mehl, H. Eckert, S. Divilov, X. Campilongo, and S. Curtarolo, *The AFLOW Library of Crystallographic Prototypes: Part 5*. Submitted to Computational Materials Science (2026).