

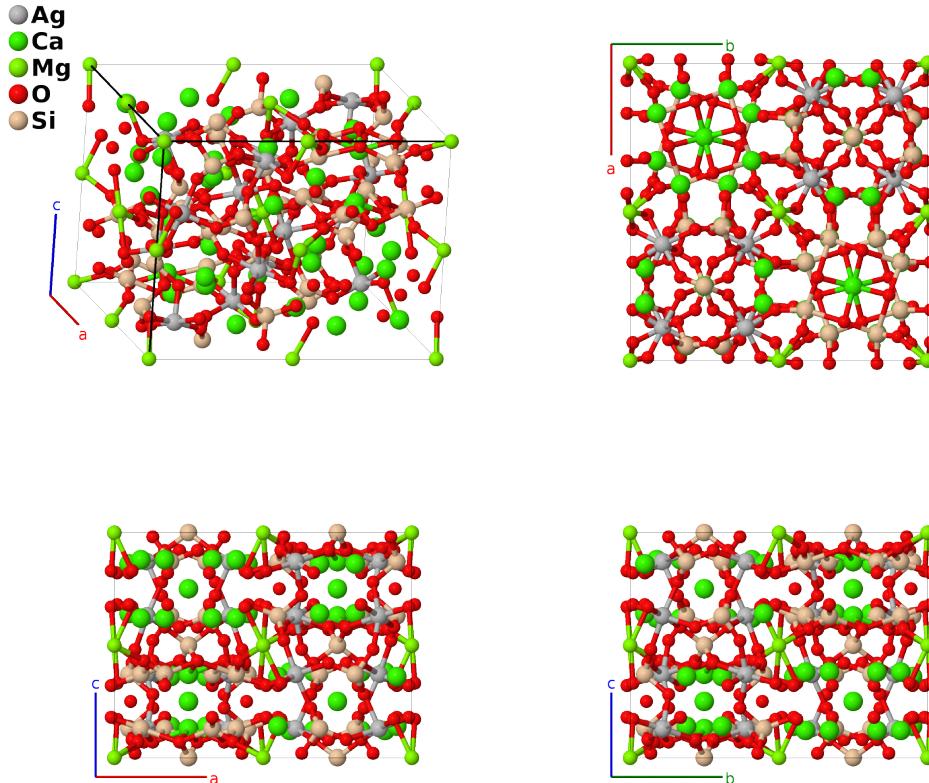
# Vesuvianite ( $\text{Ca}_{10}\text{Al}_4(\text{Mg},\text{Fe})_2\text{Si}_9\text{O}_{34}(\text{OH})_4$ , $S2_3$ ) Structure: A4B10C2D34E4F9\_tP252\_126\_k\_ce2k\_f\_h8k\_k\_d2k-001

This structure originally had the label A4B10C2D34E4F9\_tP252\_126\_k\_ce2k\_f\_h8k\_k\_d2k. Calls to that address will be redirected here.

Cite this page as: D. Hicks, M. J. Mehl, M. Esters, C. Oses, O. Levy, G. L. W. Hart, C. Toher, and S. Curtarolo, *The AFLOW Library of Crystallographic Prototypes: Part 3*, Comput. Mater. Sci. **199**, 110450 (2021), doi: 10.1016/j.commatsci.2021.110450.

<https://aflow.org/p/QSJ3>

[https://aflow.org/p/A4B10C2D34E4F9\\_tP252\\_126\\_k\\_ce2k\\_f\\_h8k\\_k\\_d2k-001](https://aflow.org/p/A4B10C2D34E4F9_tP252_126_k_ce2k_f_h8k_k_d2k-001)

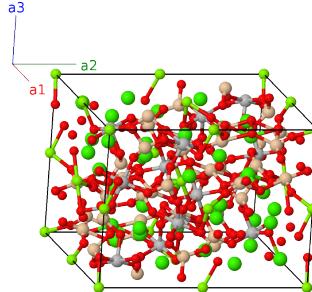


<b>Prototype</b>	$\text{Ag}_4\text{Ca}_{10}\text{Mg}_2\text{O}_{34}(\text{OH})_4\text{Si}_9$
<b>AFLOW prototype label</b>	A4B10C2D34E4F9_tP252_126_k_ce2k_f_h8k_k_d2k-001
<b>Strukturbericht designation</b>	$S2_3$
<b>Mineral name</b>	vesuvianite
<b>ICSD</b>	36198
<b>Pearson symbol</b>	tP252
<b>Space group number</b>	126
<b>Space group symbol</b>	$P4/nnc$
<b>AFLOW prototype command</b>	<pre>aflow --proto=A4B10C2D34E4F9_tP252_126_k_ce2k_f_h8k_k_d2k-001 --params=a,c/a,z3,x5,x6,y6,z6,x7,y7,z7,x8,y8,z8,x9,y9,z9,x10,y10,z10,x11,y11, z11,x12,y12,z12,x13,y13,z13,x14,y14,z14,x15,y15,z15,x16,y16,z16,x17,y17,z17,x18,y18,z18, x19,y19,z19</pre>

- Vesuvianite, also known as idocrase, comes in a variety of compositions and structures, see *e.g.*, (Allen, 1992) and (Rucklidge, 1975) and references therein. For our example we use the original structure of (Warren, 1931), where the magnesium (8f) site is filled by a random (Mg,Fe) alloy.
- The positions of the hydrogen atoms in the OH ions were not determined, so we only give the positions of the oxygen atoms (labeled as OH).

### Simple Tetragonal primitive vectors

$$\begin{aligned}\mathbf{a}_1 &= a \hat{\mathbf{x}} \\ \mathbf{a}_2 &= a \hat{\mathbf{y}} \\ \mathbf{a}_3 &= c \hat{\mathbf{z}}\end{aligned}$$



### Basis vectors

	Lattice coordinates	=	Cartesian coordinates	Wyckoff position	Atom type
$\mathbf{B}_1$	$\frac{1}{4} \mathbf{a}_1 + \frac{3}{4} \mathbf{a}_2 + \frac{3}{4} \mathbf{a}_3$	=	$\frac{1}{4}a \hat{\mathbf{x}} + \frac{3}{4}a \hat{\mathbf{y}} + \frac{3}{4}c \hat{\mathbf{z}}$	(4c)	Ca I
$\mathbf{B}_2$	$\frac{3}{4} \mathbf{a}_1 + \frac{1}{4} \mathbf{a}_2 + \frac{3}{4} \mathbf{a}_3$	=	$\frac{3}{4}a \hat{\mathbf{x}} + \frac{1}{4}a \hat{\mathbf{y}} + \frac{3}{4}c \hat{\mathbf{z}}$	(4c)	Ca I
$\mathbf{B}_3$	$\frac{3}{4} \mathbf{a}_1 + \frac{1}{4} \mathbf{a}_2 + \frac{1}{4} \mathbf{a}_3$	=	$\frac{3}{4}a \hat{\mathbf{x}} + \frac{1}{4}a \hat{\mathbf{y}} + \frac{1}{4}c \hat{\mathbf{z}}$	(4c)	Ca I
$\mathbf{B}_4$	$\frac{1}{4} \mathbf{a}_1 + \frac{3}{4} \mathbf{a}_2 + \frac{1}{4} \mathbf{a}_3$	=	$\frac{1}{4}a \hat{\mathbf{x}} + \frac{3}{4}a \hat{\mathbf{y}} + \frac{1}{4}c \hat{\mathbf{z}}$	(4c)	Ca I
$\mathbf{B}_5$	$\frac{1}{4} \mathbf{a}_1 + \frac{3}{4} \mathbf{a}_2$	=	$\frac{1}{4}a \hat{\mathbf{x}} + \frac{3}{4}a \hat{\mathbf{y}}$	(4d)	Si I
$\mathbf{B}_6$	$\frac{3}{4} \mathbf{a}_1 + \frac{1}{4} \mathbf{a}_2$	=	$\frac{3}{4}a \hat{\mathbf{x}} + \frac{1}{4}a \hat{\mathbf{y}}$	(4d)	Si I
$\mathbf{B}_7$	$\frac{1}{4} \mathbf{a}_1 + \frac{3}{4} \mathbf{a}_2 + \frac{1}{2} \mathbf{a}_3$	=	$\frac{1}{4}a \hat{\mathbf{x}} + \frac{3}{4}a \hat{\mathbf{y}} + \frac{1}{2}c \hat{\mathbf{z}}$	(4d)	Si I
$\mathbf{B}_8$	$\frac{3}{4} \mathbf{a}_1 + \frac{1}{4} \mathbf{a}_2 + \frac{1}{2} \mathbf{a}_3$	=	$\frac{3}{4}a \hat{\mathbf{x}} + \frac{1}{4}a \hat{\mathbf{y}} + \frac{1}{2}c \hat{\mathbf{z}}$	(4d)	Si I
$\mathbf{B}_9$	$\frac{1}{4} \mathbf{a}_1 + \frac{1}{4} \mathbf{a}_2 + z_3 \mathbf{a}_3$	=	$\frac{1}{4}a \hat{\mathbf{x}} + \frac{1}{4}a \hat{\mathbf{y}} + cz_3 \hat{\mathbf{z}}$	(4e)	Ca II
$\mathbf{B}_{10}$	$\frac{1}{4} \mathbf{a}_1 + \frac{1}{4} \mathbf{a}_2 - (z_3 - \frac{1}{2}) \mathbf{a}_3$	=	$\frac{1}{4}a \hat{\mathbf{x}} + \frac{1}{4}a \hat{\mathbf{y}} - c(z_3 - \frac{1}{2}) \hat{\mathbf{z}}$	(4e)	Ca II
$\mathbf{B}_{11}$	$\frac{3}{4} \mathbf{a}_1 + \frac{3}{4} \mathbf{a}_2 - z_3 \mathbf{a}_3$	=	$\frac{3}{4}a \hat{\mathbf{x}} + \frac{3}{4}a \hat{\mathbf{y}} - cz_3 \hat{\mathbf{z}}$	(4e)	Ca II
$\mathbf{B}_{12}$	$\frac{3}{4} \mathbf{a}_1 + \frac{3}{4} \mathbf{a}_2 + (z_3 + \frac{1}{2}) \mathbf{a}_3$	=	$\frac{3}{4}a \hat{\mathbf{x}} + \frac{3}{4}a \hat{\mathbf{y}} + c(z_3 + \frac{1}{2}) \hat{\mathbf{z}}$	(4e)	Ca II
$\mathbf{B}_{13}$	0	=	0	(8f)	Mg I
$\mathbf{B}_{14}$	$\frac{1}{2} \mathbf{a}_1 + \frac{1}{2} \mathbf{a}_2$	=	$\frac{1}{2}a \hat{\mathbf{x}} + \frac{1}{2}a \hat{\mathbf{y}}$	(8f)	Mg I
$\mathbf{B}_{15}$	$\frac{1}{2} \mathbf{a}_1$	=	$\frac{1}{2}a \hat{\mathbf{x}}$	(8f)	Mg I
$\mathbf{B}_{16}$	$\frac{1}{2} \mathbf{a}_2$	=	$\frac{1}{2}a \hat{\mathbf{y}}$	(8f)	Mg I
$\mathbf{B}_{17}$	$\frac{1}{2} \mathbf{a}_1 + \frac{1}{2} \mathbf{a}_3$	=	$\frac{1}{2}a \hat{\mathbf{x}} + \frac{1}{2}c \hat{\mathbf{z}}$	(8f)	Mg I
$\mathbf{B}_{18}$	$\frac{1}{2} \mathbf{a}_2 + \frac{1}{2} \mathbf{a}_3$	=	$\frac{1}{2}a \hat{\mathbf{y}} + \frac{1}{2}c \hat{\mathbf{z}}$	(8f)	Mg I
$\mathbf{B}_{19}$	$\frac{1}{2} \mathbf{a}_3$	=	$\frac{1}{2}c \hat{\mathbf{z}}$	(8f)	Mg I
$\mathbf{B}_{20}$	$\frac{1}{2} \mathbf{a}_1 + \frac{1}{2} \mathbf{a}_2 + \frac{1}{2} \mathbf{a}_3$	=	$\frac{1}{2}a \hat{\mathbf{x}} + \frac{1}{2}a \hat{\mathbf{y}} + \frac{1}{2}c \hat{\mathbf{z}}$	(8f)	Mg I
$\mathbf{B}_{21}$	$x_5 \mathbf{a}_1 + x_5 \mathbf{a}_2 + \frac{1}{4} \mathbf{a}_3$	=	$ax_5 \hat{\mathbf{x}} + ax_5 \hat{\mathbf{y}} + \frac{1}{4}c \hat{\mathbf{z}}$	(8h)	O I
$\mathbf{B}_{22}$	$-(x_5 - \frac{1}{2}) \mathbf{a}_1 - (x_5 - \frac{1}{2}) \mathbf{a}_2 + \frac{1}{4} \mathbf{a}_3$	=	$-a(x_5 - \frac{1}{2}) \hat{\mathbf{x}} - a(x_5 - \frac{1}{2}) \hat{\mathbf{y}} + \frac{1}{4}c \hat{\mathbf{z}}$	(8h)	O I

$\mathbf{B}_{23}$	$=$	$-(x_5 - \frac{1}{2}) \mathbf{a}_1 + x_5 \mathbf{a}_2 + \frac{1}{4} \mathbf{a}_3$	$=$	$-a(x_5 - \frac{1}{2}) \hat{\mathbf{x}} + ax_5 \hat{\mathbf{y}} + \frac{1}{4}c \hat{\mathbf{z}}$	(8h)	O I
$\mathbf{B}_{24}$	$=$	$x_5 \mathbf{a}_1 - (x_5 - \frac{1}{2}) \mathbf{a}_2 + \frac{1}{4} \mathbf{a}_3$	$=$	$ax_5 \hat{\mathbf{x}} - a(x_5 - \frac{1}{2}) \hat{\mathbf{y}} + \frac{1}{4}c \hat{\mathbf{z}}$	(8h)	O I
$\mathbf{B}_{25}$	$=$	$-x_5 \mathbf{a}_1 - x_5 \mathbf{a}_2 + \frac{3}{4} \mathbf{a}_3$	$=$	$-ax_5 \hat{\mathbf{x}} - ax_5 \hat{\mathbf{y}} + \frac{3}{4}c \hat{\mathbf{z}}$	(8h)	O I
$\mathbf{B}_{26}$	$=$	$(x_5 + \frac{1}{2}) \mathbf{a}_1 + (x_5 + \frac{1}{2}) \mathbf{a}_2 + \frac{3}{4} \mathbf{a}_3$	$=$	$a(x_5 + \frac{1}{2}) \hat{\mathbf{x}} + a(x_5 + \frac{1}{2}) \hat{\mathbf{y}} + \frac{3}{4}c \hat{\mathbf{z}}$	(8h)	O I
$\mathbf{B}_{27}$	$=$	$(x_5 + \frac{1}{2}) \mathbf{a}_1 - x_5 \mathbf{a}_2 + \frac{3}{4} \mathbf{a}_3$	$=$	$a(x_5 + \frac{1}{2}) \hat{\mathbf{x}} - ax_5 \hat{\mathbf{y}} + \frac{3}{4}c \hat{\mathbf{z}}$	(8h)	O I
$\mathbf{B}_{28}$	$=$	$-x_5 \mathbf{a}_1 + (x_5 + \frac{1}{2}) \mathbf{a}_2 + \frac{3}{4} \mathbf{a}_3$	$=$	$-ax_5 \hat{\mathbf{x}} + a(x_5 + \frac{1}{2}) \hat{\mathbf{y}} + \frac{3}{4}c \hat{\mathbf{z}}$	(8h)	O I
$\mathbf{B}_{29}$	$=$	$x_6 \mathbf{a}_1 + y_6 \mathbf{a}_2 + z_6 \mathbf{a}_3$	$=$	$ax_6 \hat{\mathbf{x}} + ay_6 \hat{\mathbf{y}} + cz_6 \hat{\mathbf{z}}$	(16k)	Ag I
$\mathbf{B}_{30}$	$=$	$-(x_6 - \frac{1}{2}) \mathbf{a}_1 - (y_6 - \frac{1}{2}) \mathbf{a}_2 + z_6 \mathbf{a}_3$	$=$	$-a(x_6 - \frac{1}{2}) \hat{\mathbf{x}} - a(y_6 - \frac{1}{2}) \hat{\mathbf{y}} + cz_6 \hat{\mathbf{z}}$	(16k)	Ag I
$\mathbf{B}_{31}$	$=$	$-(y_6 - \frac{1}{2}) \mathbf{a}_1 + x_6 \mathbf{a}_2 + z_6 \mathbf{a}_3$	$=$	$-a(y_6 - \frac{1}{2}) \hat{\mathbf{x}} + ax_6 \hat{\mathbf{y}} + cz_6 \hat{\mathbf{z}}$	(16k)	Ag I
$\mathbf{B}_{32}$	$=$	$y_6 \mathbf{a}_1 - (x_6 - \frac{1}{2}) \mathbf{a}_2 + z_6 \mathbf{a}_3$	$=$	$ay_6 \hat{\mathbf{x}} - a(x_6 - \frac{1}{2}) \hat{\mathbf{y}} + cz_6 \hat{\mathbf{z}}$	(16k)	Ag I
$\mathbf{B}_{33}$	$=$	$-(x_6 - \frac{1}{2}) \mathbf{a}_1 + y_6 \mathbf{a}_2 - (z_6 - \frac{1}{2}) \mathbf{a}_3$	$=$	$-a(x_6 - \frac{1}{2}) \hat{\mathbf{x}} + ay_6 \hat{\mathbf{y}} - c(z_6 - \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	Ag I
$\mathbf{B}_{34}$	$=$	$x_6 \mathbf{a}_1 - (y_6 - \frac{1}{2}) \mathbf{a}_2 - (z_6 - \frac{1}{2}) \mathbf{a}_3$	$=$	$ax_6 \hat{\mathbf{x}} - a(y_6 - \frac{1}{2}) \hat{\mathbf{y}} - c(z_6 - \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	Ag I
$\mathbf{B}_{35}$	$=$	$y_6 \mathbf{a}_1 + x_6 \mathbf{a}_2 - (z_6 - \frac{1}{2}) \mathbf{a}_3$	$=$	$ay_6 \hat{\mathbf{x}} + ax_6 \hat{\mathbf{y}} - c(z_6 - \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	Ag I
$\mathbf{B}_{36}$	$=$	$-(y_6 - \frac{1}{2}) \mathbf{a}_1 - (x_6 - \frac{1}{2}) \mathbf{a}_2 - (z_6 - \frac{1}{2}) \mathbf{a}_3$	$=$	$-a(y_6 - \frac{1}{2}) \hat{\mathbf{x}} - a(x_6 - \frac{1}{2}) \hat{\mathbf{y}} - c(z_6 - \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	Ag I
$\mathbf{B}_{37}$	$=$	$-x_6 \mathbf{a}_1 - y_6 \mathbf{a}_2 - z_6 \mathbf{a}_3$	$=$	$-ax_6 \hat{\mathbf{x}} - ay_6 \hat{\mathbf{y}} - cz_6 \hat{\mathbf{z}}$	(16k)	Ag I
$\mathbf{B}_{38}$	$=$	$(x_6 + \frac{1}{2}) \mathbf{a}_1 + (y_6 + \frac{1}{2}) \mathbf{a}_2 - z_6 \mathbf{a}_3$	$=$	$a(x_6 + \frac{1}{2}) \hat{\mathbf{x}} + a(y_6 + \frac{1}{2}) \hat{\mathbf{y}} - cz_6 \hat{\mathbf{z}}$	(16k)	Ag I
$\mathbf{B}_{39}$	$=$	$(y_6 + \frac{1}{2}) \mathbf{a}_1 - x_6 \mathbf{a}_2 - z_6 \mathbf{a}_3$	$=$	$a(y_6 + \frac{1}{2}) \hat{\mathbf{x}} - ax_6 \hat{\mathbf{y}} - cz_6 \hat{\mathbf{z}}$	(16k)	Ag I
$\mathbf{B}_{40}$	$=$	$-y_6 \mathbf{a}_1 + (x_6 + \frac{1}{2}) \mathbf{a}_2 - z_6 \mathbf{a}_3$	$=$	$-ay_6 \hat{\mathbf{x}} + a(x_6 + \frac{1}{2}) \hat{\mathbf{y}} - cz_6 \hat{\mathbf{z}}$	(16k)	Ag I
$\mathbf{B}_{41}$	$=$	$(x_6 + \frac{1}{2}) \mathbf{a}_1 - y_6 \mathbf{a}_2 + (z_6 + \frac{1}{2}) \mathbf{a}_3$	$=$	$a(x_6 + \frac{1}{2}) \hat{\mathbf{x}} - ay_6 \hat{\mathbf{y}} + c(z_6 + \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	Ag I
$\mathbf{B}_{42}$	$=$	$-x_6 \mathbf{a}_1 + (y_6 + \frac{1}{2}) \mathbf{a}_2 + (z_6 + \frac{1}{2}) \mathbf{a}_3$	$=$	$-ax_6 \hat{\mathbf{x}} + a(y_6 + \frac{1}{2}) \hat{\mathbf{y}} + c(z_6 + \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	Ag I
$\mathbf{B}_{43}$	$=$	$-y_6 \mathbf{a}_1 - x_6 \mathbf{a}_2 + (z_6 + \frac{1}{2}) \mathbf{a}_3$	$=$	$-ay_6 \hat{\mathbf{x}} - ax_6 \hat{\mathbf{y}} + c(z_6 + \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	Ag I
$\mathbf{B}_{44}$	$=$	$(y_6 + \frac{1}{2}) \mathbf{a}_1 + (x_6 + \frac{1}{2}) \mathbf{a}_2 + (z_6 + \frac{1}{2}) \mathbf{a}_3$	$=$	$a(y_6 + \frac{1}{2}) \hat{\mathbf{x}} + a(x_6 + \frac{1}{2}) \hat{\mathbf{y}} + c(z_6 + \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	Ag I
$\mathbf{B}_{45}$	$=$	$x_7 \mathbf{a}_1 + y_7 \mathbf{a}_2 + z_7 \mathbf{a}_3$	$=$	$ax_7 \hat{\mathbf{x}} + ay_7 \hat{\mathbf{y}} + cz_7 \hat{\mathbf{z}}$	(16k)	Ca III
$\mathbf{B}_{46}$	$=$	$-(x_7 - \frac{1}{2}) \mathbf{a}_1 - (y_7 - \frac{1}{2}) \mathbf{a}_2 + z_7 \mathbf{a}_3$	$=$	$-a(x_7 - \frac{1}{2}) \hat{\mathbf{x}} - a(y_7 - \frac{1}{2}) \hat{\mathbf{y}} + cz_7 \hat{\mathbf{z}}$	(16k)	Ca III
$\mathbf{B}_{47}$	$=$	$-(y_7 - \frac{1}{2}) \mathbf{a}_1 + x_7 \mathbf{a}_2 + z_7 \mathbf{a}_3$	$=$	$-a(y_7 - \frac{1}{2}) \hat{\mathbf{x}} + ax_7 \hat{\mathbf{y}} + cz_7 \hat{\mathbf{z}}$	(16k)	Ca III
$\mathbf{B}_{48}$	$=$	$y_7 \mathbf{a}_1 - (x_7 - \frac{1}{2}) \mathbf{a}_2 + z_7 \mathbf{a}_3$	$=$	$ay_7 \hat{\mathbf{x}} - a(x_7 - \frac{1}{2}) \hat{\mathbf{y}} + cz_7 \hat{\mathbf{z}}$	(16k)	Ca III
$\mathbf{B}_{49}$	$=$	$-(x_7 - \frac{1}{2}) \mathbf{a}_1 + y_7 \mathbf{a}_2 - (z_7 - \frac{1}{2}) \mathbf{a}_3$	$=$	$-a(x_7 - \frac{1}{2}) \hat{\mathbf{x}} + ay_7 \hat{\mathbf{y}} - c(z_7 - \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	Ca III
$\mathbf{B}_{50}$	$=$	$x_7 \mathbf{a}_1 - (y_7 - \frac{1}{2}) \mathbf{a}_2 - (z_7 - \frac{1}{2}) \mathbf{a}_3$	$=$	$ax_7 \hat{\mathbf{x}} - a(y_7 - \frac{1}{2}) \hat{\mathbf{y}} - c(z_7 - \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	Ca III
$\mathbf{B}_{51}$	$=$	$y_7 \mathbf{a}_1 + x_7 \mathbf{a}_2 - (z_7 - \frac{1}{2}) \mathbf{a}_3$	$=$	$ay_7 \hat{\mathbf{x}} + ax_7 \hat{\mathbf{y}} - c(z_7 - \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	Ca III
$\mathbf{B}_{52}$	$=$	$-(y_7 - \frac{1}{2}) \mathbf{a}_1 - (x_7 - \frac{1}{2}) \mathbf{a}_2 - (z_7 - \frac{1}{2}) \mathbf{a}_3$	$=$	$-a(y_7 - \frac{1}{2}) \hat{\mathbf{x}} - a(x_7 - \frac{1}{2}) \hat{\mathbf{y}} - c(z_7 - \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	Ca III
$\mathbf{B}_{53}$	$=$	$-x_7 \mathbf{a}_1 - y_7 \mathbf{a}_2 - z_7 \mathbf{a}_3$	$=$	$-ax_7 \hat{\mathbf{x}} - ay_7 \hat{\mathbf{y}} - cz_7 \hat{\mathbf{z}}$	(16k)	Ca III
$\mathbf{B}_{54}$	$=$	$(x_7 + \frac{1}{2}) \mathbf{a}_1 + (y_7 + \frac{1}{2}) \mathbf{a}_2 - z_7 \mathbf{a}_3$	$=$	$a(x_7 + \frac{1}{2}) \hat{\mathbf{x}} + a(y_7 + \frac{1}{2}) \hat{\mathbf{y}} - cz_7 \hat{\mathbf{z}}$	(16k)	Ca III
$\mathbf{B}_{55}$	$=$	$(y_7 + \frac{1}{2}) \mathbf{a}_1 - x_7 \mathbf{a}_2 - z_7 \mathbf{a}_3$	$=$	$a(y_7 + \frac{1}{2}) \hat{\mathbf{x}} - ax_7 \hat{\mathbf{y}} - cz_7 \hat{\mathbf{z}}$	(16k)	Ca III
$\mathbf{B}_{56}$	$=$	$-y_7 \mathbf{a}_1 + (x_7 + \frac{1}{2}) \mathbf{a}_2 - z_7 \mathbf{a}_3$	$=$	$-ay_7 \hat{\mathbf{x}} + a(x_7 + \frac{1}{2}) \hat{\mathbf{y}} - cz_7 \hat{\mathbf{z}}$	(16k)	Ca III
$\mathbf{B}_{57}$	$=$	$(x_7 + \frac{1}{2}) \mathbf{a}_1 - y_7 \mathbf{a}_2 + (z_7 + \frac{1}{2}) \mathbf{a}_3$	$=$	$a(x_7 + \frac{1}{2}) \hat{\mathbf{x}} - ay_7 \hat{\mathbf{y}} + c(z_7 + \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	Ca III

$\mathbf{B}_{58}$	$-x_7 \mathbf{a}_1 + (y_7 + \frac{1}{2}) \mathbf{a}_2 + (z_7 + \frac{1}{2}) \mathbf{a}_3$	$=$	$-ax_7 \hat{\mathbf{x}} + a(y_7 + \frac{1}{2}) \hat{\mathbf{y}} + c(z_7 + \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	Ca III
$\mathbf{B}_{59}$	$-y_7 \mathbf{a}_1 - x_7 \mathbf{a}_2 + (z_7 + \frac{1}{2}) \mathbf{a}_3$	$=$	$-ay_7 \hat{\mathbf{x}} - ax_7 \hat{\mathbf{y}} + c(z_7 + \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	Ca III
$\mathbf{B}_{60}$	$(y_7 + \frac{1}{2}) \mathbf{a}_1 + (x_7 + \frac{1}{2}) \mathbf{a}_2 + (z_7 + \frac{1}{2}) \mathbf{a}_3$	$=$	$a(y_7 + \frac{1}{2}) \hat{\mathbf{x}} + a(x_7 + \frac{1}{2}) \hat{\mathbf{y}} + c(z_7 + \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	Ca III
$\mathbf{B}_{61}$	$x_8 \mathbf{a}_1 + y_8 \mathbf{a}_2 + z_8 \mathbf{a}_3$	$=$	$ax_8 \hat{\mathbf{x}} + ay_8 \hat{\mathbf{y}} + cz_8 \hat{\mathbf{z}}$	(16k)	Ca IV
$\mathbf{B}_{62}$	$-(x_8 - \frac{1}{2}) \mathbf{a}_1 - (y_8 - \frac{1}{2}) \mathbf{a}_2 + z_8 \mathbf{a}_3$	$=$	$-a(x_8 - \frac{1}{2}) \hat{\mathbf{x}} - a(y_8 - \frac{1}{2}) \hat{\mathbf{y}} + cz_8 \hat{\mathbf{z}}$	(16k)	Ca IV
$\mathbf{B}_{63}$	$-(y_8 - \frac{1}{2}) \mathbf{a}_1 + x_8 \mathbf{a}_2 + z_8 \mathbf{a}_3$	$=$	$-a(y_8 - \frac{1}{2}) \hat{\mathbf{x}} + ax_8 \hat{\mathbf{y}} + cz_8 \hat{\mathbf{z}}$	(16k)	Ca IV
$\mathbf{B}_{64}$	$y_8 \mathbf{a}_1 - (x_8 - \frac{1}{2}) \mathbf{a}_2 + z_8 \mathbf{a}_3$	$=$	$ay_8 \hat{\mathbf{x}} - a(x_8 - \frac{1}{2}) \hat{\mathbf{y}} + cz_8 \hat{\mathbf{z}}$	(16k)	Ca IV
$\mathbf{B}_{65}$	$-(x_8 - \frac{1}{2}) \mathbf{a}_1 + y_8 \mathbf{a}_2 - (z_8 - \frac{1}{2}) \mathbf{a}_3$	$=$	$-a(x_8 - \frac{1}{2}) \hat{\mathbf{x}} + ay_8 \hat{\mathbf{y}} - c(z_8 - \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	Ca IV
$\mathbf{B}_{66}$	$x_8 \mathbf{a}_1 - (y_8 - \frac{1}{2}) \mathbf{a}_2 - (z_8 - \frac{1}{2}) \mathbf{a}_3$	$=$	$ax_8 \hat{\mathbf{x}} - a(y_8 - \frac{1}{2}) \hat{\mathbf{y}} - c(z_8 - \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	Ca IV
$\mathbf{B}_{67}$	$y_8 \mathbf{a}_1 + x_8 \mathbf{a}_2 - (z_8 - \frac{1}{2}) \mathbf{a}_3$	$=$	$ay_8 \hat{\mathbf{x}} + ax_8 \hat{\mathbf{y}} - c(z_8 - \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	Ca IV
$\mathbf{B}_{68}$	$-(y_8 - \frac{1}{2}) \mathbf{a}_1 - (x_8 - \frac{1}{2}) \mathbf{a}_2 - (z_8 - \frac{1}{2}) \mathbf{a}_3$	$=$	$-a(y_8 - \frac{1}{2}) \hat{\mathbf{x}} - a(x_8 - \frac{1}{2}) \hat{\mathbf{y}} - c(z_8 - \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	Ca IV
$\mathbf{B}_{69}$	$-x_8 \mathbf{a}_1 - y_8 \mathbf{a}_2 - z_8 \mathbf{a}_3$	$=$	$-ax_8 \hat{\mathbf{x}} - ay_8 \hat{\mathbf{y}} - cz_8 \hat{\mathbf{z}}$	(16k)	Ca IV
$\mathbf{B}_{70}$	$(x_8 + \frac{1}{2}) \mathbf{a}_1 + (y_8 + \frac{1}{2}) \mathbf{a}_2 - z_8 \mathbf{a}_3$	$=$	$a(x_8 + \frac{1}{2}) \hat{\mathbf{x}} + a(y_8 + \frac{1}{2}) \hat{\mathbf{y}} - cz_8 \hat{\mathbf{z}}$	(16k)	Ca IV
$\mathbf{B}_{71}$	$(y_8 + \frac{1}{2}) \mathbf{a}_1 - x_8 \mathbf{a}_2 - z_8 \mathbf{a}_3$	$=$	$a(y_8 + \frac{1}{2}) \hat{\mathbf{x}} - ax_8 \hat{\mathbf{y}} - cz_8 \hat{\mathbf{z}}$	(16k)	Ca IV
$\mathbf{B}_{72}$	$-y_8 \mathbf{a}_1 + (x_8 + \frac{1}{2}) \mathbf{a}_2 - z_8 \mathbf{a}_3$	$=$	$-ay_8 \hat{\mathbf{x}} + a(x_8 + \frac{1}{2}) \hat{\mathbf{y}} - cz_8 \hat{\mathbf{z}}$	(16k)	Ca IV
$\mathbf{B}_{73}$	$(x_8 + \frac{1}{2}) \mathbf{a}_1 - y_8 \mathbf{a}_2 + (z_8 + \frac{1}{2}) \mathbf{a}_3$	$=$	$a(x_8 + \frac{1}{2}) \hat{\mathbf{x}} - ay_8 \hat{\mathbf{y}} + c(z_8 + \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	Ca IV
$\mathbf{B}_{74}$	$-x_8 \mathbf{a}_1 + (y_8 + \frac{1}{2}) \mathbf{a}_2 + (z_8 + \frac{1}{2}) \mathbf{a}_3$	$=$	$-ax_8 \hat{\mathbf{x}} + a(y_8 + \frac{1}{2}) \hat{\mathbf{y}} + c(z_8 + \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	Ca IV
$\mathbf{B}_{75}$	$-y_8 \mathbf{a}_1 - x_8 \mathbf{a}_2 + (z_8 + \frac{1}{2}) \mathbf{a}_3$	$=$	$-ay_8 \hat{\mathbf{x}} - ax_8 \hat{\mathbf{y}} + c(z_8 + \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	Ca IV
$\mathbf{B}_{76}$	$(y_8 + \frac{1}{2}) \mathbf{a}_1 + (x_8 + \frac{1}{2}) \mathbf{a}_2 + (z_8 + \frac{1}{2}) \mathbf{a}_3$	$=$	$a(y_8 + \frac{1}{2}) \hat{\mathbf{x}} + a(x_8 + \frac{1}{2}) \hat{\mathbf{y}} + c(z_8 + \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	Ca IV
$\mathbf{B}_{77}$	$x_9 \mathbf{a}_1 + y_9 \mathbf{a}_2 + z_9 \mathbf{a}_3$	$=$	$ax_9 \hat{\mathbf{x}} + ay_9 \hat{\mathbf{y}} + cz_9 \hat{\mathbf{z}}$	(16k)	O II
$\mathbf{B}_{78}$	$-(x_9 - \frac{1}{2}) \mathbf{a}_1 - (y_9 - \frac{1}{2}) \mathbf{a}_2 + z_9 \mathbf{a}_3$	$=$	$-a(x_9 - \frac{1}{2}) \hat{\mathbf{x}} - a(y_9 - \frac{1}{2}) \hat{\mathbf{y}} + cz_9 \hat{\mathbf{z}}$	(16k)	O II
$\mathbf{B}_{79}$	$-(y_9 - \frac{1}{2}) \mathbf{a}_1 + x_9 \mathbf{a}_2 + z_9 \mathbf{a}_3$	$=$	$-a(y_9 - \frac{1}{2}) \hat{\mathbf{x}} + ax_9 \hat{\mathbf{y}} + cz_9 \hat{\mathbf{z}}$	(16k)	O II
$\mathbf{B}_{80}$	$y_9 \mathbf{a}_1 - (x_9 - \frac{1}{2}) \mathbf{a}_2 + z_9 \mathbf{a}_3$	$=$	$ay_9 \hat{\mathbf{x}} - a(x_9 - \frac{1}{2}) \hat{\mathbf{y}} + cz_9 \hat{\mathbf{z}}$	(16k)	O II
$\mathbf{B}_{81}$	$-(x_9 - \frac{1}{2}) \mathbf{a}_1 + y_9 \mathbf{a}_2 - (z_9 - \frac{1}{2}) \mathbf{a}_3$	$=$	$-a(x_9 - \frac{1}{2}) \hat{\mathbf{x}} + ay_9 \hat{\mathbf{y}} - c(z_9 - \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	O II
$\mathbf{B}_{82}$	$x_9 \mathbf{a}_1 - (y_9 - \frac{1}{2}) \mathbf{a}_2 - (z_9 - \frac{1}{2}) \mathbf{a}_3$	$=$	$ax_9 \hat{\mathbf{x}} - a(y_9 - \frac{1}{2}) \hat{\mathbf{y}} - c(z_9 - \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	O II
$\mathbf{B}_{83}$	$y_9 \mathbf{a}_1 + x_9 \mathbf{a}_2 - (z_9 - \frac{1}{2}) \mathbf{a}_3$	$=$	$ay_9 \hat{\mathbf{x}} + ax_9 \hat{\mathbf{y}} - c(z_9 - \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	O II
$\mathbf{B}_{84}$	$-(y_9 - \frac{1}{2}) \mathbf{a}_1 - (x_9 - \frac{1}{2}) \mathbf{a}_2 - (z_9 - \frac{1}{2}) \mathbf{a}_3$	$=$	$-a(y_9 - \frac{1}{2}) \hat{\mathbf{x}} - a(x_9 - \frac{1}{2}) \hat{\mathbf{y}} - c(z_9 - \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	O II
$\mathbf{B}_{85}$	$-x_9 \mathbf{a}_1 - y_9 \mathbf{a}_2 - z_9 \mathbf{a}_3$	$=$	$-ax_9 \hat{\mathbf{x}} - ay_9 \hat{\mathbf{y}} - cz_9 \hat{\mathbf{z}}$	(16k)	O II
$\mathbf{B}_{86}$	$(x_9 + \frac{1}{2}) \mathbf{a}_1 + (y_9 + \frac{1}{2}) \mathbf{a}_2 - z_9 \mathbf{a}_3$	$=$	$a(x_9 + \frac{1}{2}) \hat{\mathbf{x}} + a(y_9 + \frac{1}{2}) \hat{\mathbf{y}} - cz_9 \hat{\mathbf{z}}$	(16k)	O II
$\mathbf{B}_{87}$	$(y_9 + \frac{1}{2}) \mathbf{a}_1 - x_9 \mathbf{a}_2 - z_9 \mathbf{a}_3$	$=$	$a(y_9 + \frac{1}{2}) \hat{\mathbf{x}} - ax_9 \hat{\mathbf{y}} - cz_9 \hat{\mathbf{z}}$	(16k)	O II
$\mathbf{B}_{88}$	$-y_9 \mathbf{a}_1 + (x_9 + \frac{1}{2}) \mathbf{a}_2 - z_9 \mathbf{a}_3$	$=$	$-ay_9 \hat{\mathbf{x}} + a(x_9 + \frac{1}{2}) \hat{\mathbf{y}} - cz_9 \hat{\mathbf{z}}$	(16k)	O II
$\mathbf{B}_{89}$	$(x_9 + \frac{1}{2}) \mathbf{a}_1 - y_9 \mathbf{a}_2 + (z_9 + \frac{1}{2}) \mathbf{a}_3$	$=$	$a(x_9 + \frac{1}{2}) \hat{\mathbf{x}} - ay_9 \hat{\mathbf{y}} + c(z_9 + \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	O II
$\mathbf{B}_{90}$	$-x_9 \mathbf{a}_1 + (y_9 + \frac{1}{2}) \mathbf{a}_2 + (z_9 + \frac{1}{2}) \mathbf{a}_3$	$=$	$-ax_9 \hat{\mathbf{x}} + a(y_9 + \frac{1}{2}) \hat{\mathbf{y}} + c(z_9 + \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	O II



$\mathbf{B}_{121} =$	$(x_{11} + \frac{1}{2}) \mathbf{a}_1 - y_{11} \mathbf{a}_2 + (z_{11} + \frac{1}{2}) \mathbf{a}_3$	$=$	$a(x_{11} + \frac{1}{2}) \hat{\mathbf{x}} - ay_{11} \hat{\mathbf{y}} + c(z_{11} + \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	O IV
$\mathbf{B}_{122} =$	$-x_{11} \mathbf{a}_1 + (y_{11} + \frac{1}{2}) \mathbf{a}_2 + (z_{11} + \frac{1}{2}) \mathbf{a}_3$	$=$	$-ax_{11} \hat{\mathbf{x}} + a(y_{11} + \frac{1}{2}) \hat{\mathbf{y}} + c(z_{11} + \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	O IV
$\mathbf{B}_{123} =$	$-y_{11} \mathbf{a}_1 - x_{11} \mathbf{a}_2 + (z_{11} + \frac{1}{2}) \mathbf{a}_3$	$=$	$-ay_{11} \hat{\mathbf{x}} - ax_{11} \hat{\mathbf{y}} + c(z_{11} + \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	O IV
$\mathbf{B}_{124} =$	$(y_{11} + \frac{1}{2}) \mathbf{a}_1 + (x_{11} + \frac{1}{2}) \mathbf{a}_2 + (z_{11} + \frac{1}{2}) \mathbf{a}_3$	$=$	$a(y_{11} + \frac{1}{2}) \hat{\mathbf{x}} + a(x_{11} + \frac{1}{2}) \hat{\mathbf{y}} + c(z_{11} + \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	O IV
$\mathbf{B}_{125} =$	$x_{12} \mathbf{a}_1 + y_{12} \mathbf{a}_2 + z_{12} \mathbf{a}_3$	$=$	$ax_{12} \hat{\mathbf{x}} + ay_{12} \hat{\mathbf{y}} + cz_{12} \hat{\mathbf{z}}$	(16k)	O V
$\mathbf{B}_{126} =$	$-(x_{12} - \frac{1}{2}) \mathbf{a}_1 - (y_{12} - \frac{1}{2}) \mathbf{a}_2 + z_{12} \mathbf{a}_3$	$=$	$-a(x_{12} - \frac{1}{2}) \hat{\mathbf{x}} - a(y_{12} - \frac{1}{2}) \hat{\mathbf{y}} + cz_{12} \hat{\mathbf{z}}$	(16k)	O V
$\mathbf{B}_{127} =$	$-(y_{12} - \frac{1}{2}) \mathbf{a}_1 + x_{12} \mathbf{a}_2 + z_{12} \mathbf{a}_3$	$=$	$-a(y_{12} - \frac{1}{2}) \hat{\mathbf{x}} + ax_{12} \hat{\mathbf{y}} + cz_{12} \hat{\mathbf{z}}$	(16k)	O V
$\mathbf{B}_{128} =$	$y_{12} \mathbf{a}_1 - (x_{12} - \frac{1}{2}) \mathbf{a}_2 + z_{12} \mathbf{a}_3$	$=$	$ay_{12} \hat{\mathbf{x}} - a(x_{12} - \frac{1}{2}) \hat{\mathbf{y}} + cz_{12} \hat{\mathbf{z}}$	(16k)	O V
$\mathbf{B}_{129} =$	$-(x_{12} - \frac{1}{2}) \mathbf{a}_1 + y_{12} \mathbf{a}_2 - (z_{12} - \frac{1}{2}) \mathbf{a}_3$	$=$	$-a(x_{12} - \frac{1}{2}) \hat{\mathbf{x}} + ay_{12} \hat{\mathbf{y}} - c(z_{12} - \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	O V
$\mathbf{B}_{130} =$	$x_{12} \mathbf{a}_1 - (y_{12} - \frac{1}{2}) \mathbf{a}_2 - (z_{12} - \frac{1}{2}) \mathbf{a}_3$	$=$	$ax_{12} \hat{\mathbf{x}} - a(y_{12} - \frac{1}{2}) \hat{\mathbf{y}} - c(z_{12} - \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	O V
$\mathbf{B}_{131} =$	$y_{12} \mathbf{a}_1 + x_{12} \mathbf{a}_2 - (z_{12} - \frac{1}{2}) \mathbf{a}_3$	$=$	$ay_{12} \hat{\mathbf{x}} + ax_{12} \hat{\mathbf{y}} - c(z_{12} - \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	O V
$\mathbf{B}_{132} =$	$-(y_{12} - \frac{1}{2}) \mathbf{a}_1 - (x_{12} - \frac{1}{2}) \mathbf{a}_2 - (z_{12} - \frac{1}{2}) \mathbf{a}_3$	$=$	$-a(y_{12} - \frac{1}{2}) \hat{\mathbf{x}} - a(x_{12} - \frac{1}{2}) \hat{\mathbf{y}} - c(z_{12} - \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	O V
$\mathbf{B}_{133} =$	$-x_{12} \mathbf{a}_1 - y_{12} \mathbf{a}_2 - z_{12} \mathbf{a}_3$	$=$	$-ax_{12} \hat{\mathbf{x}} - ay_{12} \hat{\mathbf{y}} - cz_{12} \hat{\mathbf{z}}$	(16k)	O V
$\mathbf{B}_{134} =$	$(x_{12} + \frac{1}{2}) \mathbf{a}_1 + (y_{12} + \frac{1}{2}) \mathbf{a}_2 - z_{12} \mathbf{a}_3$	$=$	$a(x_{12} + \frac{1}{2}) \hat{\mathbf{x}} + a(y_{12} + \frac{1}{2}) \hat{\mathbf{y}} - cz_{12} \hat{\mathbf{z}}$	(16k)	O V
$\mathbf{B}_{135} =$	$(y_{12} + \frac{1}{2}) \mathbf{a}_1 - x_{12} \mathbf{a}_2 - z_{12} \mathbf{a}_3$	$=$	$a(y_{12} + \frac{1}{2}) \hat{\mathbf{x}} - ax_{12} \hat{\mathbf{y}} - cz_{12} \hat{\mathbf{z}}$	(16k)	O V
$\mathbf{B}_{136} =$	$-y_{12} \mathbf{a}_1 + (x_{12} + \frac{1}{2}) \mathbf{a}_2 - z_{12} \mathbf{a}_3$	$=$	$-ay_{12} \hat{\mathbf{x}} + a(x_{12} + \frac{1}{2}) \hat{\mathbf{y}} - cz_{12} \hat{\mathbf{z}}$	(16k)	O V
$\mathbf{B}_{137} =$	$(x_{12} + \frac{1}{2}) \mathbf{a}_1 - y_{12} \mathbf{a}_2 + (z_{12} + \frac{1}{2}) \mathbf{a}_3$	$=$	$a(x_{12} + \frac{1}{2}) \hat{\mathbf{x}} - ay_{12} \hat{\mathbf{y}} + c(z_{12} + \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	O V
$\mathbf{B}_{138} =$	$-x_{12} \mathbf{a}_1 + (y_{12} + \frac{1}{2}) \mathbf{a}_2 + (z_{12} + \frac{1}{2}) \mathbf{a}_3$	$=$	$-ax_{12} \hat{\mathbf{x}} + a(y_{12} + \frac{1}{2}) \hat{\mathbf{y}} + c(z_{12} + \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	O V
$\mathbf{B}_{139} =$	$-y_{12} \mathbf{a}_1 - x_{12} \mathbf{a}_2 + (z_{12} + \frac{1}{2}) \mathbf{a}_3$	$=$	$-ay_{12} \hat{\mathbf{x}} - ax_{12} \hat{\mathbf{y}} + c(z_{12} + \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	O V
$\mathbf{B}_{140} =$	$(y_{12} + \frac{1}{2}) \mathbf{a}_1 + (x_{12} + \frac{1}{2}) \mathbf{a}_2 + (z_{12} + \frac{1}{2}) \mathbf{a}_3$	$=$	$a(y_{12} + \frac{1}{2}) \hat{\mathbf{x}} + a(x_{12} + \frac{1}{2}) \hat{\mathbf{y}} + c(z_{12} + \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	O V
$\mathbf{B}_{141} =$	$x_{13} \mathbf{a}_1 + y_{13} \mathbf{a}_2 + z_{13} \mathbf{a}_3$	$=$	$ax_{13} \hat{\mathbf{x}} + ay_{13} \hat{\mathbf{y}} + cz_{13} \hat{\mathbf{z}}$	(16k)	O VI
$\mathbf{B}_{142} =$	$-(x_{13} - \frac{1}{2}) \mathbf{a}_1 - (y_{13} - \frac{1}{2}) \mathbf{a}_2 + z_{13} \mathbf{a}_3$	$=$	$-a(x_{13} - \frac{1}{2}) \hat{\mathbf{x}} - a(y_{13} - \frac{1}{2}) \hat{\mathbf{y}} + cz_{13} \hat{\mathbf{z}}$	(16k)	O VI
$\mathbf{B}_{143} =$	$-(y_{13} - \frac{1}{2}) \mathbf{a}_1 + x_{13} \mathbf{a}_2 + z_{13} \mathbf{a}_3$	$=$	$-a(y_{13} - \frac{1}{2}) \hat{\mathbf{x}} + ax_{13} \hat{\mathbf{y}} + cz_{13} \hat{\mathbf{z}}$	(16k)	O VI
$\mathbf{B}_{144} =$	$y_{13} \mathbf{a}_1 - (x_{13} - \frac{1}{2}) \mathbf{a}_2 + z_{13} \mathbf{a}_3$	$=$	$ay_{13} \hat{\mathbf{x}} - a(x_{13} - \frac{1}{2}) \hat{\mathbf{y}} + cz_{13} \hat{\mathbf{z}}$	(16k)	O VI
$\mathbf{B}_{145} =$	$-(x_{13} - \frac{1}{2}) \mathbf{a}_1 + y_{13} \mathbf{a}_2 - (z_{13} - \frac{1}{2}) \mathbf{a}_3$	$=$	$-a(x_{13} - \frac{1}{2}) \hat{\mathbf{x}} + ay_{13} \hat{\mathbf{y}} - c(z_{13} - \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	O VI
$\mathbf{B}_{146} =$	$x_{13} \mathbf{a}_1 - (y_{13} - \frac{1}{2}) \mathbf{a}_2 - (z_{13} - \frac{1}{2}) \mathbf{a}_3$	$=$	$ax_{13} \hat{\mathbf{x}} - a(y_{13} - \frac{1}{2}) \hat{\mathbf{y}} - c(z_{13} - \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	O VI
$\mathbf{B}_{147} =$	$y_{13} \mathbf{a}_1 + x_{13} \mathbf{a}_2 - (z_{13} - \frac{1}{2}) \mathbf{a}_3$	$=$	$ay_{13} \hat{\mathbf{x}} + ax_{13} \hat{\mathbf{y}} - c(z_{13} - \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	O VI
$\mathbf{B}_{148} =$	$-(y_{13} - \frac{1}{2}) \mathbf{a}_1 - (x_{13} - \frac{1}{2}) \mathbf{a}_2 - (z_{13} - \frac{1}{2}) \mathbf{a}_3$	$=$	$-a(y_{13} - \frac{1}{2}) \hat{\mathbf{x}} - a(x_{13} - \frac{1}{2}) \hat{\mathbf{y}} - c(z_{13} - \frac{1}{2}) \hat{\mathbf{z}}$	(16k)	O VI
$\mathbf{B}_{149} =$	$-x_{13} \mathbf{a}_1 - y_{13} \mathbf{a}_2 - z_{13} \mathbf{a}_3$	$=$	$-ax_{13} \hat{\mathbf{x}} - ay_{13} \hat{\mathbf{y}} - cz_{13} \hat{\mathbf{z}}$	(16k)	O VI





$\mathbf{B}_{210} =$	$x_{17}\mathbf{a}_1 - (y_{17} - \frac{1}{2})\mathbf{a}_2 - (z_{17} - \frac{1}{2})\mathbf{a}_3$	$=$	$ax_{17}\hat{\mathbf{x}} - a(y_{17} - \frac{1}{2})\hat{\mathbf{y}} - c(z_{17} - \frac{1}{2})\hat{\mathbf{z}}$	(16k)	OH I
$\mathbf{B}_{211} =$	$y_{17}\mathbf{a}_1 + x_{17}\mathbf{a}_2 - (z_{17} - \frac{1}{2})\mathbf{a}_3$	$=$	$ay_{17}\hat{\mathbf{x}} + ax_{17}\hat{\mathbf{y}} - c(z_{17} - \frac{1}{2})\hat{\mathbf{z}}$	(16k)	OH I
$\mathbf{B}_{212} =$	$-(y_{17} - \frac{1}{2})\mathbf{a}_1 - (x_{17} - \frac{1}{2})\mathbf{a}_2 - (z_{17} - \frac{1}{2})\mathbf{a}_3$	$=$	$-a(y_{17} - \frac{1}{2})\hat{\mathbf{x}} - a(x_{17} - \frac{1}{2})\hat{\mathbf{y}} - c(z_{17} - \frac{1}{2})\hat{\mathbf{z}}$	(16k)	OH I
$\mathbf{B}_{213} =$	$-x_{17}\mathbf{a}_1 - y_{17}\mathbf{a}_2 - z_{17}\mathbf{a}_3$	$=$	$-ax_{17}\hat{\mathbf{x}} - ay_{17}\hat{\mathbf{y}} - cz_{17}\hat{\mathbf{z}}$	(16k)	OH I
$\mathbf{B}_{214} =$	$(x_{17} + \frac{1}{2})\mathbf{a}_1 + (y_{17} + \frac{1}{2})\mathbf{a}_2 - z_{17}\mathbf{a}_3$	$=$	$a(x_{17} + \frac{1}{2})\hat{\mathbf{x}} + a(y_{17} + \frac{1}{2})\hat{\mathbf{y}} - cz_{17}\hat{\mathbf{z}}$	(16k)	OH I
$\mathbf{B}_{215} =$	$(y_{17} + \frac{1}{2})\mathbf{a}_1 - x_{17}\mathbf{a}_2 - z_{17}\mathbf{a}_3$	$=$	$a(y_{17} + \frac{1}{2})\hat{\mathbf{x}} - ax_{17}\hat{\mathbf{y}} - cz_{17}\hat{\mathbf{z}}$	(16k)	OH I
$\mathbf{B}_{216} =$	$-y_{17}\mathbf{a}_1 + (x_{17} + \frac{1}{2})\mathbf{a}_2 - z_{17}\mathbf{a}_3$	$=$	$-ay_{17}\hat{\mathbf{x}} + a(x_{17} + \frac{1}{2})\hat{\mathbf{y}} - cz_{17}\hat{\mathbf{z}}$	(16k)	OH I
$\mathbf{B}_{217} =$	$(x_{17} + \frac{1}{2})\mathbf{a}_1 - y_{17}\mathbf{a}_2 + (z_{17} + \frac{1}{2})\mathbf{a}_3$	$=$	$a(x_{17} + \frac{1}{2})\hat{\mathbf{x}} - ay_{17}\hat{\mathbf{y}} + c(z_{17} + \frac{1}{2})\hat{\mathbf{z}}$	(16k)	OH I
$\mathbf{B}_{218} =$	$-x_{17}\mathbf{a}_1 + (y_{17} + \frac{1}{2})\mathbf{a}_2 + (z_{17} + \frac{1}{2})\mathbf{a}_3$	$=$	$-ax_{17}\hat{\mathbf{x}} + a(y_{17} + \frac{1}{2})\hat{\mathbf{y}} + c(z_{17} + \frac{1}{2})\hat{\mathbf{z}}$	(16k)	OH I
$\mathbf{B}_{219} =$	$-y_{17}\mathbf{a}_1 - x_{17}\mathbf{a}_2 + (z_{17} + \frac{1}{2})\mathbf{a}_3$	$=$	$-ay_{17}\hat{\mathbf{x}} - ax_{17}\hat{\mathbf{y}} + c(z_{17} + \frac{1}{2})\hat{\mathbf{z}}$	(16k)	OH I
$\mathbf{B}_{220} =$	$(y_{17} + \frac{1}{2})\mathbf{a}_1 + (x_{17} + \frac{1}{2})\mathbf{a}_2 + (z_{17} + \frac{1}{2})\mathbf{a}_3$	$=$	$a(y_{17} + \frac{1}{2})\hat{\mathbf{x}} + a(x_{17} + \frac{1}{2})\hat{\mathbf{y}} + c(z_{17} + \frac{1}{2})\hat{\mathbf{z}}$	(16k)	OH I
$\mathbf{B}_{221} =$	$x_{18}\mathbf{a}_1 + y_{18}\mathbf{a}_2 + z_{18}\mathbf{a}_3$	$=$	$ax_{18}\hat{\mathbf{x}} + ay_{18}\hat{\mathbf{y}} + cz_{18}\hat{\mathbf{z}}$	(16k)	Si II
$\mathbf{B}_{222} =$	$-(x_{18} - \frac{1}{2})\mathbf{a}_1 - (y_{18} - \frac{1}{2})\mathbf{a}_2 + z_{18}\mathbf{a}_3$	$=$	$-a(x_{18} - \frac{1}{2})\hat{\mathbf{x}} - a(y_{18} - \frac{1}{2})\hat{\mathbf{y}} + cz_{18}\hat{\mathbf{z}}$	(16k)	Si II
$\mathbf{B}_{223} =$	$-(y_{18} - \frac{1}{2})\mathbf{a}_1 + x_{18}\mathbf{a}_2 + z_{18}\mathbf{a}_3$	$=$	$-a(y_{18} - \frac{1}{2})\hat{\mathbf{x}} + ax_{18}\hat{\mathbf{y}} + cz_{18}\hat{\mathbf{z}}$	(16k)	Si II
$\mathbf{B}_{224} =$	$y_{18}\mathbf{a}_1 - (x_{18} - \frac{1}{2})\mathbf{a}_2 + z_{18}\mathbf{a}_3$	$=$	$ay_{18}\hat{\mathbf{x}} - a(x_{18} - \frac{1}{2})\hat{\mathbf{y}} + cz_{18}\hat{\mathbf{z}}$	(16k)	Si II
$\mathbf{B}_{225} =$	$-(x_{18} - \frac{1}{2})\mathbf{a}_1 + y_{18}\mathbf{a}_2 - (z_{18} - \frac{1}{2})\mathbf{a}_3$	$=$	$-a(x_{18} - \frac{1}{2})\hat{\mathbf{x}} + ay_{18}\hat{\mathbf{y}} - c(z_{18} - \frac{1}{2})\hat{\mathbf{z}}$	(16k)	Si II
$\mathbf{B}_{226} =$	$x_{18}\mathbf{a}_1 - (y_{18} - \frac{1}{2})\mathbf{a}_2 - (z_{18} - \frac{1}{2})\mathbf{a}_3$	$=$	$ax_{18}\hat{\mathbf{x}} - a(y_{18} - \frac{1}{2})\hat{\mathbf{y}} - c(z_{18} - \frac{1}{2})\hat{\mathbf{z}}$	(16k)	Si II
$\mathbf{B}_{227} =$	$y_{18}\mathbf{a}_1 + x_{18}\mathbf{a}_2 - (z_{18} - \frac{1}{2})\mathbf{a}_3$	$=$	$ay_{18}\hat{\mathbf{x}} + ax_{18}\hat{\mathbf{y}} - c(z_{18} - \frac{1}{2})\hat{\mathbf{z}}$	(16k)	Si II
$\mathbf{B}_{228} =$	$-(y_{18} - \frac{1}{2})\mathbf{a}_1 - (x_{18} - \frac{1}{2})\mathbf{a}_2 - (z_{18} - \frac{1}{2})\mathbf{a}_3$	$=$	$-a(y_{18} - \frac{1}{2})\hat{\mathbf{x}} - a(x_{18} - \frac{1}{2})\hat{\mathbf{y}} - c(z_{18} - \frac{1}{2})\hat{\mathbf{z}}$	(16k)	Si II
$\mathbf{B}_{229} =$	$-x_{18}\mathbf{a}_1 - y_{18}\mathbf{a}_2 - z_{18}\mathbf{a}_3$	$=$	$-ax_{18}\hat{\mathbf{x}} - ay_{18}\hat{\mathbf{y}} - cz_{18}\hat{\mathbf{z}}$	(16k)	Si II
$\mathbf{B}_{230} =$	$(x_{18} + \frac{1}{2})\mathbf{a}_1 + (y_{18} + \frac{1}{2})\mathbf{a}_2 - z_{18}\mathbf{a}_3$	$=$	$a(x_{18} + \frac{1}{2})\hat{\mathbf{x}} + a(y_{18} + \frac{1}{2})\hat{\mathbf{y}} - cz_{18}\hat{\mathbf{z}}$	(16k)	Si II
$\mathbf{B}_{231} =$	$(y_{18} + \frac{1}{2})\mathbf{a}_1 - x_{18}\mathbf{a}_2 - z_{18}\mathbf{a}_3$	$=$	$a(y_{18} + \frac{1}{2})\hat{\mathbf{x}} - ax_{18}\hat{\mathbf{y}} - cz_{18}\hat{\mathbf{z}}$	(16k)	Si II
$\mathbf{B}_{232} =$	$-y_{18}\mathbf{a}_1 + (x_{18} + \frac{1}{2})\mathbf{a}_2 - z_{18}\mathbf{a}_3$	$=$	$-ay_{18}\hat{\mathbf{x}} + a(x_{18} + \frac{1}{2})\hat{\mathbf{y}} - cz_{18}\hat{\mathbf{z}}$	(16k)	Si II
$\mathbf{B}_{233} =$	$(x_{18} + \frac{1}{2})\mathbf{a}_1 - y_{18}\mathbf{a}_2 + (z_{18} + \frac{1}{2})\mathbf{a}_3$	$=$	$a(x_{18} + \frac{1}{2})\hat{\mathbf{x}} - ay_{18}\hat{\mathbf{y}} + c(z_{18} + \frac{1}{2})\hat{\mathbf{z}}$	(16k)	Si II
$\mathbf{B}_{234} =$	$-x_{18}\mathbf{a}_1 + (y_{18} + \frac{1}{2})\mathbf{a}_2 + (z_{18} + \frac{1}{2})\mathbf{a}_3$	$=$	$-ax_{18}\hat{\mathbf{x}} + a(y_{18} + \frac{1}{2})\hat{\mathbf{y}} + c(z_{18} + \frac{1}{2})\hat{\mathbf{z}}$	(16k)	Si II
$\mathbf{B}_{235} =$	$-y_{18}\mathbf{a}_1 - x_{18}\mathbf{a}_2 + (z_{18} + \frac{1}{2})\mathbf{a}_3$	$=$	$-ay_{18}\hat{\mathbf{x}} - ax_{18}\hat{\mathbf{y}} + c(z_{18} + \frac{1}{2})\hat{\mathbf{z}}$	(16k)	Si II
$\mathbf{B}_{236} =$	$(y_{18} + \frac{1}{2})\mathbf{a}_1 + (x_{18} + \frac{1}{2})\mathbf{a}_2 + (z_{18} + \frac{1}{2})\mathbf{a}_3$	$=$	$a(y_{18} + \frac{1}{2})\hat{\mathbf{x}} + a(x_{18} + \frac{1}{2})\hat{\mathbf{y}} + c(z_{18} + \frac{1}{2})\hat{\mathbf{z}}$	(16k)	Si II
$\mathbf{B}_{237} =$	$x_{19}\mathbf{a}_1 + y_{19}\mathbf{a}_2 + z_{19}\mathbf{a}_3$	$=$	$ax_{19}\hat{\mathbf{x}} + ay_{19}\hat{\mathbf{y}} + cz_{19}\hat{\mathbf{z}}$	(16k)	Si III
$\mathbf{B}_{238} =$	$-(x_{19} - \frac{1}{2})\mathbf{a}_1 - (y_{19} - \frac{1}{2})\mathbf{a}_2 + z_{19}\mathbf{a}_3$	$=$	$-a(x_{19} - \frac{1}{2})\hat{\mathbf{x}} - a(y_{19} - \frac{1}{2})\hat{\mathbf{y}} + cz_{19}\hat{\mathbf{z}}$	(16k)	Si III
$\mathbf{B}_{239} =$	$-(y_{19} - \frac{1}{2})\mathbf{a}_1 + x_{19}\mathbf{a}_2 + z_{19}\mathbf{a}_3$	$=$	$-a(y_{19} - \frac{1}{2})\hat{\mathbf{x}} + ax_{19}\hat{\mathbf{y}} + cz_{19}\hat{\mathbf{z}}$	(16k)	Si III

$$\begin{aligned}
\mathbf{B}_{240} &= y_{19} \mathbf{a}_1 - \left( x_{19} - \frac{1}{2} \right) \mathbf{a}_2 + z_{19} \mathbf{a}_3 & = & ay_{19} \hat{\mathbf{x}} - a \left( x_{19} - \frac{1}{2} \right) \hat{\mathbf{y}} + cz_{19} \hat{\mathbf{z}} & (16k) & \text{Si III} \\
\mathbf{B}_{241} &= - \left( x_{19} - \frac{1}{2} \right) \mathbf{a}_1 + y_{19} \mathbf{a}_2 - \left( z_{19} - \frac{1}{2} \right) \mathbf{a}_3 & = & -a \left( x_{19} - \frac{1}{2} \right) \hat{\mathbf{x}} + ay_{19} \hat{\mathbf{y}} - c \left( z_{19} - \frac{1}{2} \right) \hat{\mathbf{z}} & (16k) & \text{Si III} \\
\mathbf{B}_{242} &= x_{19} \mathbf{a}_1 - \left( y_{19} - \frac{1}{2} \right) \mathbf{a}_2 - \left( z_{19} - \frac{1}{2} \right) \mathbf{a}_3 & = & ax_{19} \hat{\mathbf{x}} - a \left( y_{19} - \frac{1}{2} \right) \hat{\mathbf{y}} - c \left( z_{19} - \frac{1}{2} \right) \hat{\mathbf{z}} & (16k) & \text{Si III} \\
\mathbf{B}_{243} &= y_{19} \mathbf{a}_1 + x_{19} \mathbf{a}_2 - \left( z_{19} - \frac{1}{2} \right) \mathbf{a}_3 & = & ay_{19} \hat{\mathbf{x}} + ax_{19} \hat{\mathbf{y}} - c \left( z_{19} - \frac{1}{2} \right) \hat{\mathbf{z}} & (16k) & \text{Si III} \\
\mathbf{B}_{244} &= - \left( y_{19} - \frac{1}{2} \right) \mathbf{a}_1 - \left( x_{19} - \frac{1}{2} \right) \mathbf{a}_2 - \left( z_{19} - \frac{1}{2} \right) \mathbf{a}_3 & = & -a \left( y_{19} - \frac{1}{2} \right) \hat{\mathbf{x}} - a \left( x_{19} - \frac{1}{2} \right) \hat{\mathbf{y}} - c \left( z_{19} - \frac{1}{2} \right) \hat{\mathbf{z}} & (16k) & \text{Si III} \\
\mathbf{B}_{245} &= -x_{19} \mathbf{a}_1 - y_{19} \mathbf{a}_2 - z_{19} \mathbf{a}_3 & = & -ax_{19} \hat{\mathbf{x}} - ay_{19} \hat{\mathbf{y}} - cz_{19} \hat{\mathbf{z}} & (16k) & \text{Si III} \\
\mathbf{B}_{246} &= \left( x_{19} + \frac{1}{2} \right) \mathbf{a}_1 + \left( y_{19} + \frac{1}{2} \right) \mathbf{a}_2 - z_{19} \mathbf{a}_3 & = & a \left( x_{19} + \frac{1}{2} \right) \hat{\mathbf{x}} + a \left( y_{19} + \frac{1}{2} \right) \hat{\mathbf{y}} - cz_{19} \hat{\mathbf{z}} & (16k) & \text{Si III} \\
\mathbf{B}_{247} &= \left( y_{19} + \frac{1}{2} \right) \mathbf{a}_1 - x_{19} \mathbf{a}_2 - z_{19} \mathbf{a}_3 & = & a \left( y_{19} + \frac{1}{2} \right) \hat{\mathbf{x}} - ax_{19} \hat{\mathbf{y}} - cz_{19} \hat{\mathbf{z}} & (16k) & \text{Si III} \\
\mathbf{B}_{248} &= -y_{19} \mathbf{a}_1 + \left( x_{19} + \frac{1}{2} \right) \mathbf{a}_2 - z_{19} \mathbf{a}_3 & = & -ay_{19} \hat{\mathbf{x}} + a \left( x_{19} + \frac{1}{2} \right) \hat{\mathbf{y}} - cz_{19} \hat{\mathbf{z}} & (16k) & \text{Si III} \\
\mathbf{B}_{249} &= \left( x_{19} + \frac{1}{2} \right) \mathbf{a}_1 - y_{19} \mathbf{a}_2 + \left( z_{19} + \frac{1}{2} \right) \mathbf{a}_3 & = & a \left( x_{19} + \frac{1}{2} \right) \hat{\mathbf{x}} - ay_{19} \hat{\mathbf{y}} + c \left( z_{19} + \frac{1}{2} \right) \hat{\mathbf{z}} & (16k) & \text{Si III} \\
\mathbf{B}_{250} &= -x_{19} \mathbf{a}_1 + \left( y_{19} + \frac{1}{2} \right) \mathbf{a}_2 + \left( z_{19} + \frac{1}{2} \right) \mathbf{a}_3 & = & -ax_{19} \hat{\mathbf{x}} + a \left( y_{19} + \frac{1}{2} \right) \hat{\mathbf{y}} + c \left( z_{19} + \frac{1}{2} \right) \hat{\mathbf{z}} & (16k) & \text{Si III} \\
\mathbf{B}_{251} &= -y_{19} \mathbf{a}_1 - x_{19} \mathbf{a}_2 + \left( z_{19} + \frac{1}{2} \right) \mathbf{a}_3 & = & -ay_{19} \hat{\mathbf{x}} - ax_{19} \hat{\mathbf{y}} + c \left( z_{19} + \frac{1}{2} \right) \hat{\mathbf{z}} & (16k) & \text{Si III} \\
\mathbf{B}_{252} &= \left( y_{19} + \frac{1}{2} \right) \mathbf{a}_1 + \left( x_{19} + \frac{1}{2} \right) \mathbf{a}_2 + \left( z_{19} + \frac{1}{2} \right) \mathbf{a}_3 & = & a \left( y_{19} + \frac{1}{2} \right) \hat{\mathbf{x}} + a \left( x_{19} + \frac{1}{2} \right) \hat{\mathbf{y}} + c \left( z_{19} + \frac{1}{2} \right) \hat{\mathbf{z}} & (16k) & \text{Si III}
\end{aligned}$$

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