

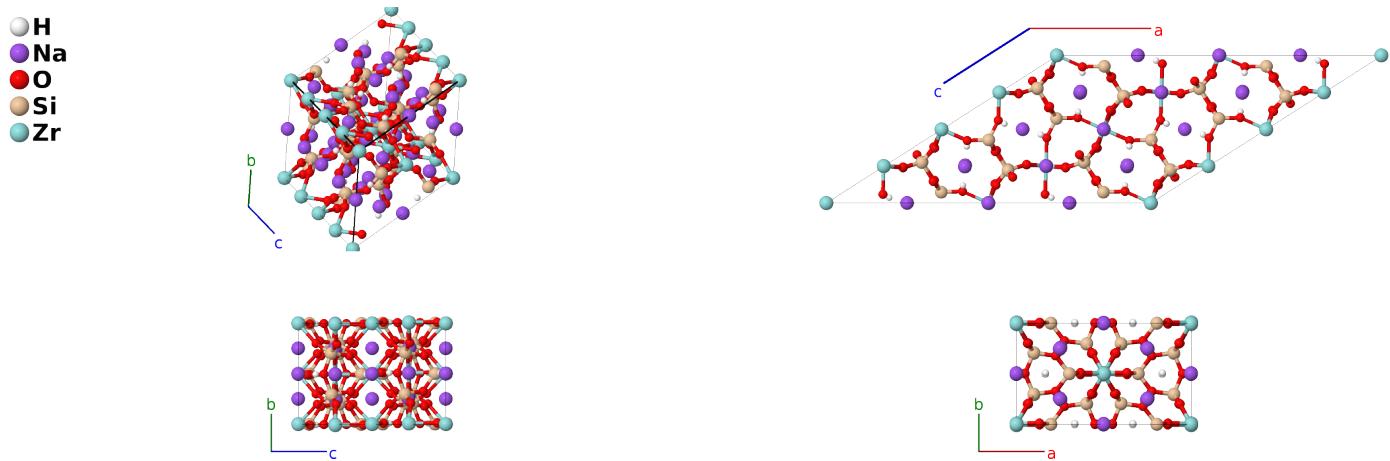
Catapleiite ($\text{Na}_2\text{ZrSi}_3\text{O}_9 \cdot 2\text{H}_2\text{O}$) Structure: A2B3C9D3E_mC144_15_2f_abcef_9f_3f_de-001

This structure originally had the label A2B3C9D3E_mC144_15_2f_bcdef_9f_3f_ae. Calls to that address will be redirected here.

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<https://aflow.org/p/L4VZ>

https://aflow.org/p/A2B3C9D3E_mC144_15_2f_abcef_9f_3f_de-001

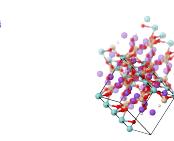


Prototype	$(\text{H}_2\text{O})_2\text{Na}_2\text{O}_9\text{Si}_3\text{Zr}$
AFLOW prototype label	A2B3C9D3E_mC144_15_2f_abcef_9f_3f_de-001
Mineral name	catapleiite
ICSD	20267
Pearson symbol	mC144
Space group number	15
Space group symbol	$C2/c$
AFLOW prototype command	<pre>aflow --proto=A2B3C9D3E_mC144_15_2f_abcef_9f_3f_de-001 --params=a,b/a,c/a,\beta,y5,y6,x7,y7,z7,x8,y8,z8,x9,y9,z9,x10,y10,z10,x11,y11,z11, x12,y12,z12,x13,y13,z13,x14,y14,z14,x15,y15,z15,x16,y16,z16,x17,y17,z17,x18,y18,z18,x19, y19,z19,x20,y20,z20,x21,y21,z21</pre>

- This is a refinement of the crystal structure of catapleiite. The original hexagonal structure was given the *Strukturbericht* designation *S3₄* by (Gottfried, 1937).
- Only 66.7% of the sodium atom sites are occupied.
- (Ilyushin, 1981) gave the lattice parameters and Wyckoff positions in terms of the *B2/b* setting of space group #15. We used findsym to transform this to the standard *C2/c* setting. This required the *y*- and *z*-axes to be swapped.
- The hydrogen positions are unknown, so the water molecules are designated H_2O .

Base-centered Monoclinic primitive vectors

$$\begin{aligned}\mathbf{a}_1 &= \frac{1}{2}a\hat{\mathbf{x}} - \frac{1}{2}b\hat{\mathbf{y}} \\ \mathbf{a}_2 &= \frac{1}{2}a\hat{\mathbf{x}} + \frac{1}{2}b\hat{\mathbf{y}} \\ \mathbf{a}_3 &= c\cos\beta\hat{\mathbf{x}} + c\sin\beta\hat{\mathbf{z}}\end{aligned}$$



Basis vectors

	Lattice coordinates	Cartesian coordinates	Wyckoff position	Atom type
\mathbf{B}_1	= 0	= 0	(4a)	Na I
\mathbf{B}_2	= $\frac{1}{2}\mathbf{a}_3$	= $\frac{1}{2}c\cos\beta\hat{\mathbf{x}} + \frac{1}{2}c\sin\beta\hat{\mathbf{z}}$	(4a)	Na I
\mathbf{B}_3	= $\frac{1}{2}\mathbf{a}_1 + \frac{1}{2}\mathbf{a}_2$	= $\frac{1}{2}a\hat{\mathbf{x}}$	(4b)	Na II
\mathbf{B}_4	= $\frac{1}{2}\mathbf{a}_1 + \frac{1}{2}\mathbf{a}_2 + \frac{1}{2}\mathbf{a}_3$	= $\frac{1}{2}(a + c\cos\beta)\hat{\mathbf{x}} + \frac{1}{2}c\sin\beta\hat{\mathbf{z}}$	(4b)	Na II
\mathbf{B}_5	= $\frac{1}{2}\mathbf{a}_2$	= $\frac{1}{4}a\hat{\mathbf{x}} + \frac{1}{4}b\hat{\mathbf{y}}$	(4c)	Na III
\mathbf{B}_6	= $\frac{1}{2}\mathbf{a}_1 + \frac{1}{2}\mathbf{a}_3$	= $\left(\frac{a}{4} + \frac{c\cos\beta}{2}\right)\hat{\mathbf{x}} - \frac{1}{4}b\hat{\mathbf{y}} + \frac{1}{2}c\sin\beta\hat{\mathbf{z}}$	(4c)	Na III
\mathbf{B}_7	= $\frac{1}{2}\mathbf{a}_2 + \frac{1}{2}\mathbf{a}_3$	= $\left(\frac{a}{4} + \frac{c\cos\beta}{2}\right)\hat{\mathbf{x}} + \frac{1}{4}b\hat{\mathbf{y}} + \frac{1}{2}c\sin\beta\hat{\mathbf{z}}$	(4d)	Zr I
\mathbf{B}_8	= $\frac{1}{2}\mathbf{a}_1$	= $\frac{1}{4}a\hat{\mathbf{x}} - \frac{1}{4}b\hat{\mathbf{y}}$	(4d)	Zr I
\mathbf{B}_9	= $-y_5\mathbf{a}_1 + y_5\mathbf{a}_2 + \frac{1}{4}\mathbf{a}_3$	= $\frac{1}{4}c\cos\beta\hat{\mathbf{x}} + by_5\hat{\mathbf{y}} + \frac{1}{4}c\sin\beta\hat{\mathbf{z}}$	(4e)	Na IV
\mathbf{B}_{10}	= $y_5\mathbf{a}_1 - y_5\mathbf{a}_2 + \frac{3}{4}\mathbf{a}_3$	= $\frac{3}{4}c\cos\beta\hat{\mathbf{x}} - by_5\hat{\mathbf{y}} + \frac{3}{4}c\sin\beta\hat{\mathbf{z}}$	(4e)	Na IV
\mathbf{B}_{11}	= $-y_6\mathbf{a}_1 + y_6\mathbf{a}_2 + \frac{1}{4}\mathbf{a}_3$	= $\frac{1}{4}c\cos\beta\hat{\mathbf{x}} + by_6\hat{\mathbf{y}} + \frac{1}{4}c\sin\beta\hat{\mathbf{z}}$	(4e)	Zr II
\mathbf{B}_{12}	= $y_6\mathbf{a}_1 - y_6\mathbf{a}_2 + \frac{3}{4}\mathbf{a}_3$	= $\frac{3}{4}c\cos\beta\hat{\mathbf{x}} - by_6\hat{\mathbf{y}} + \frac{3}{4}c\sin\beta\hat{\mathbf{z}}$	(4e)	Zr II
\mathbf{B}_{13}	= $(x_7 - y_7)\mathbf{a}_1 + (x_7 + y_7)\mathbf{a}_2 + z_7\mathbf{a}_3$	= $(ax_7 + cz_7\cos\beta)\hat{\mathbf{x}} + by_7\hat{\mathbf{y}} + cz_7\sin\beta\hat{\mathbf{z}}$	(8f)	H I
\mathbf{B}_{14}	= $-(x_7 + y_7)\mathbf{a}_1 - (x_7 - y_7)\mathbf{a}_2 - (z_7 - \frac{1}{2})\mathbf{a}_3$	= $-(ax_7 + c(z_7 - \frac{1}{2})\cos\beta)\hat{\mathbf{x}} + by_7\hat{\mathbf{y}} - c(z_7 - \frac{1}{2})\sin\beta\hat{\mathbf{z}}$	(8f)	H I
\mathbf{B}_{15}	= $-(x_7 - y_7)\mathbf{a}_1 - (x_7 + y_7)\mathbf{a}_2 - z_7\mathbf{a}_3$	= $-(ax_7 + cz_7\cos\beta)\hat{\mathbf{x}} - by_7\hat{\mathbf{y}} - cz_7\sin\beta\hat{\mathbf{z}}$	(8f)	H I
\mathbf{B}_{16}	= $(x_7 + y_7)\mathbf{a}_1 + (x_7 - y_7)\mathbf{a}_2 + (z_7 + \frac{1}{2})\mathbf{a}_3$	= $(ax_7 + c(z_7 + \frac{1}{2})\cos\beta)\hat{\mathbf{x}} - by_7\hat{\mathbf{y}} + c(z_7 + \frac{1}{2})\sin\beta\hat{\mathbf{z}}$	(8f)	H I
\mathbf{B}_{17}	= $(x_8 - y_8)\mathbf{a}_1 + (x_8 + y_8)\mathbf{a}_2 + z_8\mathbf{a}_3$	= $(ax_8 + cz_8\cos\beta)\hat{\mathbf{x}} + by_8\hat{\mathbf{y}} + cz_8\sin\beta\hat{\mathbf{z}}$	(8f)	H II
\mathbf{B}_{18}	= $-(x_8 + y_8)\mathbf{a}_1 - (x_8 - y_8)\mathbf{a}_2 - (z_8 - \frac{1}{2})\mathbf{a}_3$	= $-(ax_8 + c(z_8 - \frac{1}{2})\cos\beta)\hat{\mathbf{x}} + by_8\hat{\mathbf{y}} - c(z_8 - \frac{1}{2})\sin\beta\hat{\mathbf{z}}$	(8f)	H II
\mathbf{B}_{19}	= $-(x_8 - y_8)\mathbf{a}_1 - (x_8 + y_8)\mathbf{a}_2 - z_8\mathbf{a}_3$	= $-(ax_8 + cz_8\cos\beta)\hat{\mathbf{x}} - by_8\hat{\mathbf{y}} - cz_8\sin\beta\hat{\mathbf{z}}$	(8f)	H II
\mathbf{B}_{20}	= $(x_8 + y_8)\mathbf{a}_1 + (x_8 - y_8)\mathbf{a}_2 + (z_8 + \frac{1}{2})\mathbf{a}_3$	= $(ax_8 + c(z_8 + \frac{1}{2})\cos\beta)\hat{\mathbf{x}} - by_8\hat{\mathbf{y}} + c(z_8 + \frac{1}{2})\sin\beta\hat{\mathbf{z}}$	(8f)	H II
\mathbf{B}_{21}	= $(x_9 - y_9)\mathbf{a}_1 + (x_9 + y_9)\mathbf{a}_2 + z_9\mathbf{a}_3$	= $(ax_9 + cz_9\cos\beta)\hat{\mathbf{x}} + by_9\hat{\mathbf{y}} + cz_9\sin\beta\hat{\mathbf{z}}$	(8f)	Na V
\mathbf{B}_{22}	= $-(x_9 + y_9)\mathbf{a}_1 - (x_9 - y_9)\mathbf{a}_2 - (z_9 - \frac{1}{2})\mathbf{a}_3$	= $-(ax_9 + c(z_9 - \frac{1}{2})\cos\beta)\hat{\mathbf{x}} + by_9\hat{\mathbf{y}} - c(z_9 - \frac{1}{2})\sin\beta\hat{\mathbf{z}}$	(8f)	Na V
\mathbf{B}_{23}	= $-(x_9 - y_9)\mathbf{a}_1 - (x_9 + y_9)\mathbf{a}_2 - z_9\mathbf{a}_3$	= $-(ax_9 + cz_9\cos\beta)\hat{\mathbf{x}} - by_9\hat{\mathbf{y}} - cz_9\sin\beta\hat{\mathbf{z}}$	(8f)	Na V
\mathbf{B}_{24}	= $(x_9 + y_9)\mathbf{a}_1 + (x_9 - y_9)\mathbf{a}_2 + (z_9 + \frac{1}{2})\mathbf{a}_3$	= $(ax_9 + c(z_9 + \frac{1}{2})\cos\beta)\hat{\mathbf{x}} - by_9\hat{\mathbf{y}} + c(z_9 + \frac{1}{2})\sin\beta\hat{\mathbf{z}}$	(8f)	Na V

\mathbf{B}_{25}	$(x_{10} - y_{10}) \mathbf{a}_1 +$ $(x_{10} + y_{10}) \mathbf{a}_2 + z_{10} \mathbf{a}_3$	$= (ax_{10} + cz_{10} \cos \beta) \hat{\mathbf{x}} + by_{10} \hat{\mathbf{y}} + cz_{10} \sin \beta \hat{\mathbf{z}}$	(8f)	O I
\mathbf{B}_{26}	$-(x_{10} + y_{10}) \mathbf{a}_1 -$ $(x_{10} - y_{10}) \mathbf{a}_2 - (z_{10} - \frac{1}{2}) \mathbf{a}_3$	$= -(ax_{10} + c(z_{10} - \frac{1}{2}) \cos \beta) \hat{\mathbf{x}} + by_{10} \hat{\mathbf{y}} -$ $c(z_{10} - \frac{1}{2}) \sin \beta \hat{\mathbf{z}}$	(8f)	O I
\mathbf{B}_{27}	$-(x_{10} - y_{10}) \mathbf{a}_1 -$ $(x_{10} + y_{10}) \mathbf{a}_2 - z_{10} \mathbf{a}_3$	$= -(ax_{10} + cz_{10} \cos \beta) \hat{\mathbf{x}} - by_{10} \hat{\mathbf{y}} -$ $cz_{10} \sin \beta \hat{\mathbf{z}}$	(8f)	O I
\mathbf{B}_{28}	$(x_{10} + y_{10}) \mathbf{a}_1 +$ $(x_{10} - y_{10}) \mathbf{a}_2 + (z_{10} + \frac{1}{2}) \mathbf{a}_3$	$= (ax_{10} + c(z_{10} + \frac{1}{2}) \cos \beta) \hat{\mathbf{x}} - by_{10} \hat{\mathbf{y}} +$ $c(z_{10} + \frac{1}{2}) \sin \beta \hat{\mathbf{z}}$	(8f)	O I
\mathbf{B}_{29}	$(x_{11} - y_{11}) \mathbf{a}_1 +$ $(x_{11} + y_{11}) \mathbf{a}_2 + z_{11} \mathbf{a}_3$	$= (ax_{11} + cz_{11} \cos \beta) \hat{\mathbf{x}} + by_{11} \hat{\mathbf{y}} + cz_{11} \sin \beta \hat{\mathbf{z}}$	(8f)	O II
\mathbf{B}_{30}	$-(x_{11} + y_{11}) \mathbf{a}_1 -$ $(x_{11} - y_{11}) \mathbf{a}_2 - (z_{11} - \frac{1}{2}) \mathbf{a}_3$	$= -(ax_{11} + c(z_{11} - \frac{1}{2}) \cos \beta) \hat{\mathbf{x}} + by_{11} \hat{\mathbf{y}} -$ $c(z_{11} - \frac{1}{2}) \sin \beta \hat{\mathbf{z}}$	(8f)	O II
\mathbf{B}_{31}	$-(x_{11} - y_{11}) \mathbf{a}_1 -$ $(x_{11} + y_{11}) \mathbf{a}_2 - z_{11} \mathbf{a}_3$	$= -(ax_{11} + cz_{11} \cos \beta) \hat{\mathbf{x}} - by_{11} \hat{\mathbf{y}} -$ $cz_{11} \sin \beta \hat{\mathbf{z}}$	(8f)	O II
\mathbf{B}_{32}	$(x_{11} + y_{11}) \mathbf{a}_1 +$ $(x_{11} - y_{11}) \mathbf{a}_2 + (z_{11} + \frac{1}{2}) \mathbf{a}_3$	$= (ax_{11} + c(z_{11} + \frac{1}{2}) \cos \beta) \hat{\mathbf{x}} - by_{11} \hat{\mathbf{y}} +$ $c(z_{11} + \frac{1}{2}) \sin \beta \hat{\mathbf{z}}$	(8f)	O II
\mathbf{B}_{33}	$(x_{12} - y_{12}) \mathbf{a}_1 +$ $(x_{12} + y_{12}) \mathbf{a}_2 + z_{12} \mathbf{a}_3$	$= (ax_{12} + cz_{12} \cos \beta) \hat{\mathbf{x}} + by_{12} \hat{\mathbf{y}} + cz_{12} \sin \beta \hat{\mathbf{z}}$	(8f)	O III
\mathbf{B}_{34}	$-(x_{12} + y_{12}) \mathbf{a}_1 -$ $(x_{12} - y_{12}) \mathbf{a}_2 - (z_{12} - \frac{1}{2}) \mathbf{a}_3$	$= -(ax_{12} + c(z_{12} - \frac{1}{2}) \cos \beta) \hat{\mathbf{x}} + by_{12} \hat{\mathbf{y}} -$ $c(z_{12} - \frac{1}{2}) \sin \beta \hat{\mathbf{z}}$	(8f)	O III
\mathbf{B}_{35}	$-(x_{12} - y_{12}) \mathbf{a}_1 -$ $(x_{12} + y_{12}) \mathbf{a}_2 - z_{12} \mathbf{a}_3$	$= -(ax_{12} + cz_{12} \cos \beta) \hat{\mathbf{x}} - by_{12} \hat{\mathbf{y}} -$ $cz_{12} \sin \beta \hat{\mathbf{z}}$	(8f)	O III
\mathbf{B}_{36}	$(x_{12} + y_{12}) \mathbf{a}_1 +$ $(x_{12} - y_{12}) \mathbf{a}_2 + (z_{12} + \frac{1}{2}) \mathbf{a}_3$	$= (ax_{12} + c(z_{12} + \frac{1}{2}) \cos \beta) \hat{\mathbf{x}} - by_{12} \hat{\mathbf{y}} +$ $c(z_{12} + \frac{1}{2}) \sin \beta \hat{\mathbf{z}}$	(8f)	O III
\mathbf{B}_{37}	$(x_{13} - y_{13}) \mathbf{a}_1 +$ $(x_{13} + y_{13}) \mathbf{a}_2 + z_{13} \mathbf{a}_3$	$= (ax_{13} + cz_{13} \cos \beta) \hat{\mathbf{x}} + by_{13} \hat{\mathbf{y}} + cz_{13} \sin \beta \hat{\mathbf{z}}$	(8f)	O IV
\mathbf{B}_{38}	$-(x_{13} + y_{13}) \mathbf{a}_1 -$ $(x_{13} - y_{13}) \mathbf{a}_2 - (z_{13} - \frac{1}{2}) \mathbf{a}_3$	$= -(ax_{13} + c(z_{13} - \frac{1}{2}) \cos \beta) \hat{\mathbf{x}} + by_{13} \hat{\mathbf{y}} -$ $c(z_{13} - \frac{1}{2}) \sin \beta \hat{\mathbf{z}}$	(8f)	O IV
\mathbf{B}_{39}	$-(x_{13} - y_{13}) \mathbf{a}_1 -$ $(x_{13} + y_{13}) \mathbf{a}_2 - z_{13} \mathbf{a}_3$	$= -(ax_{13} + cz_{13} \cos \beta) \hat{\mathbf{x}} - by_{13} \hat{\mathbf{y}} -$ $cz_{13} \sin \beta \hat{\mathbf{z}}$	(8f)	O IV
\mathbf{B}_{40}	$(x_{13} + y_{13}) \mathbf{a}_1 +$ $(x_{13} - y_{13}) \mathbf{a}_2 + (z_{13} + \frac{1}{2}) \mathbf{a}_3$	$= (ax_{13} + c(z_{13} + \frac{1}{2}) \cos \beta) \hat{\mathbf{x}} - by_{13} \hat{\mathbf{y}} +$ $c(z_{13} + \frac{1}{2}) \sin \beta \hat{\mathbf{z}}$	(8f)	O IV
\mathbf{B}_{41}	$(x_{14} - y_{14}) \mathbf{a}_1 +$ $(x_{14} + y_{14}) \mathbf{a}_2 + z_{14} \mathbf{a}_3$	$= (ax_{14} + cz_{14} \cos \beta) \hat{\mathbf{x}} + by_{14} \hat{\mathbf{y}} + cz_{14} \sin \beta \hat{\mathbf{z}}$	(8f)	O V
\mathbf{B}_{42}	$-(x_{14} + y_{14}) \mathbf{a}_1 -$ $(x_{14} - y_{14}) \mathbf{a}_2 - (z_{14} - \frac{1}{2}) \mathbf{a}_3$	$= -(ax_{14} + c(z_{14} - \frac{1}{2}) \cos \beta) \hat{\mathbf{x}} + by_{14} \hat{\mathbf{y}} -$ $c(z_{14} - \frac{1}{2}) \sin \beta \hat{\mathbf{z}}$	(8f)	O V
\mathbf{B}_{43}	$-(x_{14} - y_{14}) \mathbf{a}_1 -$ $(x_{14} + y_{14}) \mathbf{a}_2 - z_{14} \mathbf{a}_3$	$= -(ax_{14} + cz_{14} \cos \beta) \hat{\mathbf{x}} - by_{14} \hat{\mathbf{y}} -$ $cz_{14} \sin \beta \hat{\mathbf{z}}$	(8f)	O V
\mathbf{B}_{44}	$(x_{14} + y_{14}) \mathbf{a}_1 +$ $(x_{14} - y_{14}) \mathbf{a}_2 + (z_{14} + \frac{1}{2}) \mathbf{a}_3$	$= (ax_{14} + c(z_{14} + \frac{1}{2}) \cos \beta) \hat{\mathbf{x}} - by_{14} \hat{\mathbf{y}} +$ $c(z_{14} + \frac{1}{2}) \sin \beta \hat{\mathbf{z}}$	(8f)	O V
\mathbf{B}_{45}	$(x_{15} - y_{15}) \mathbf{a}_1 +$ $(x_{15} + y_{15}) \mathbf{a}_2 + z_{15} \mathbf{a}_3$	$= (ax_{15} + cz_{15} \cos \beta) \hat{\mathbf{x}} + by_{15} \hat{\mathbf{y}} + cz_{15} \sin \beta \hat{\mathbf{z}}$	(8f)	O VI
\mathbf{B}_{46}	$-(x_{15} + y_{15}) \mathbf{a}_1 -$ $(x_{15} - y_{15}) \mathbf{a}_2 - (z_{15} - \frac{1}{2}) \mathbf{a}_3$	$= -(ax_{15} + c(z_{15} - \frac{1}{2}) \cos \beta) \hat{\mathbf{x}} + by_{15} \hat{\mathbf{y}} -$ $c(z_{15} - \frac{1}{2}) \sin \beta \hat{\mathbf{z}}$	(8f)	O VI
\mathbf{B}_{47}	$-(x_{15} - y_{15}) \mathbf{a}_1 -$ $(x_{15} + y_{15}) \mathbf{a}_2 - z_{15} \mathbf{a}_3$	$= -(ax_{15} + cz_{15} \cos \beta) \hat{\mathbf{x}} - by_{15} \hat{\mathbf{y}} -$ $cz_{15} \sin \beta \hat{\mathbf{z}}$	(8f)	O VI

\mathbf{B}_{48}	$(x_{15} + y_{15}) \mathbf{a}_1 +$ $(x_{15} - y_{15}) \mathbf{a}_2 + (z_{15} + \frac{1}{2}) \mathbf{a}_3$	$= (ax_{15} + c(z_{15} + \frac{1}{2}) \cos \beta) \hat{\mathbf{x}} - by_{15} \hat{\mathbf{y}} +$ $c(z_{15} + \frac{1}{2}) \sin \beta \hat{\mathbf{z}}$	(8f)	O VI
\mathbf{B}_{49}	$(x_{16} - y_{16}) \mathbf{a}_1 +$ $(x_{16} + y_{16}) \mathbf{a}_2 + z_{16} \mathbf{a}_3$	$= (ax_{16} + cz_{16} \cos \beta) \hat{\mathbf{x}} + by_{16} \hat{\mathbf{y}} + cz_{16} \sin \beta \hat{\mathbf{z}}$	(8f)	O VII
\mathbf{B}_{50}	$-(x_{16} + y_{16}) \mathbf{a}_1 -$ $(x_{16} - y_{16}) \mathbf{a}_2 - (z_{16} - \frac{1}{2}) \mathbf{a}_3$	$= -(ax_{16} + c(z_{16} - \frac{1}{2}) \cos \beta) \hat{\mathbf{x}} + by_{16} \hat{\mathbf{y}} -$ $c(z_{16} - \frac{1}{2}) \sin \beta \hat{\mathbf{z}}$	(8f)	O VII
\mathbf{B}_{51}	$-(x_{16} - y_{16}) \mathbf{a}_1 -$ $(x_{16} + y_{16}) \mathbf{a}_2 - z_{16} \mathbf{a}_3$	$= -(ax_{16} + cz_{16} \cos \beta) \hat{\mathbf{x}} - by_{16} \hat{\mathbf{y}} -$ $cz_{16} \sin \beta \hat{\mathbf{z}}$	(8f)	O VII
\mathbf{B}_{52}	$(x_{16} + y_{16}) \mathbf{a}_1 +$ $(x_{16} - y_{16}) \mathbf{a}_2 + (z_{16} + \frac{1}{2}) \mathbf{a}_3$	$= (ax_{16} + c(z_{16} + \frac{1}{2}) \cos \beta) \hat{\mathbf{x}} - by_{16} \hat{\mathbf{y}} +$ $c(z_{16} + \frac{1}{2}) \sin \beta \hat{\mathbf{z}}$	(8f)	O VII
\mathbf{B}_{53}	$(x_{17} - y_{17}) \mathbf{a}_1 +$ $(x_{17} + y_{17}) \mathbf{a}_2 + z_{17} \mathbf{a}_3$	$= (ax_{17} + cz_{17} \cos \beta) \hat{\mathbf{x}} + by_{17} \hat{\mathbf{y}} + cz_{17} \sin \beta \hat{\mathbf{z}}$	(8f)	O VIII
\mathbf{B}_{54}	$-(x_{17} + y_{17}) \mathbf{a}_1 -$ $(x_{17} - y_{17}) \mathbf{a}_2 - (z_{17} - \frac{1}{2}) \mathbf{a}_3$	$= -(ax_{17} + c(z_{17} - \frac{1}{2}) \cos \beta) \hat{\mathbf{x}} + by_{17} \hat{\mathbf{y}} -$ $c(z_{17} - \frac{1}{2}) \sin \beta \hat{\mathbf{z}}$	(8f)	O VIII
\mathbf{B}_{55}	$-(x_{17} - y_{17}) \mathbf{a}_1 -$ $(x_{17} + y_{17}) \mathbf{a}_2 - z_{17} \mathbf{a}_3$	$= -(ax_{17} + cz_{17} \cos \beta) \hat{\mathbf{x}} - by_{17} \hat{\mathbf{y}} -$ $cz_{17} \sin \beta \hat{\mathbf{z}}$	(8f)	O VIII
\mathbf{B}_{56}	$(x_{17} + y_{17}) \mathbf{a}_1 +$ $(x_{17} - y_{17}) \mathbf{a}_2 + (z_{17} + \frac{1}{2}) \mathbf{a}_3$	$= (ax_{17} + c(z_{17} + \frac{1}{2}) \cos \beta) \hat{\mathbf{x}} - by_{17} \hat{\mathbf{y}} +$ $c(z_{17} + \frac{1}{2}) \sin \beta \hat{\mathbf{z}}$	(8f)	O VIII
\mathbf{B}_{57}	$(x_{18} - y_{18}) \mathbf{a}_1 +$ $(x_{18} + y_{18}) \mathbf{a}_2 + z_{18} \mathbf{a}_3$	$= (ax_{18} + cz_{18} \cos \beta) \hat{\mathbf{x}} + by_{18} \hat{\mathbf{y}} + cz_{18} \sin \beta \hat{\mathbf{z}}$	(8f)	O IX
\mathbf{B}_{58}	$-(x_{18} + y_{18}) \mathbf{a}_1 -$ $(x_{18} - y_{18}) \mathbf{a}_2 - (z_{18} - \frac{1}{2}) \mathbf{a}_3$	$= -(ax_{18} + c(z_{18} - \frac{1}{2}) \cos \beta) \hat{\mathbf{x}} + by_{18} \hat{\mathbf{y}} -$ $c(z_{18} - \frac{1}{2}) \sin \beta \hat{\mathbf{z}}$	(8f)	O IX
\mathbf{B}_{59}	$-(x_{18} - y_{18}) \mathbf{a}_1 -$ $(x_{18} + y_{18}) \mathbf{a}_2 - z_{18} \mathbf{a}_3$	$= -(ax_{18} + cz_{18} \cos \beta) \hat{\mathbf{x}} - by_{18} \hat{\mathbf{y}} -$ $cz_{18} \sin \beta \hat{\mathbf{z}}$	(8f)	O IX
\mathbf{B}_{60}	$(x_{18} + y_{18}) \mathbf{a}_1 +$ $(x_{18} - y_{18}) \mathbf{a}_2 + (z_{18} + \frac{1}{2}) \mathbf{a}_3$	$= (ax_{18} + c(z_{18} + \frac{1}{2}) \cos \beta) \hat{\mathbf{x}} - by_{18} \hat{\mathbf{y}} +$ $c(z_{18} + \frac{1}{2}) \sin \beta \hat{\mathbf{z}}$	(8f)	O IX
\mathbf{B}_{61}	$(x_{19} - y_{19}) \mathbf{a}_1 +$ $(x_{19} + y_{19}) \mathbf{a}_2 + z_{19} \mathbf{a}_3$	$= (ax_{19} + cz_{19} \cos \beta) \hat{\mathbf{x}} + by_{19} \hat{\mathbf{y}} + cz_{19} \sin \beta \hat{\mathbf{z}}$	(8f)	Si I
\mathbf{B}_{62}	$-(x_{19} + y_{19}) \mathbf{a}_1 -$ $(x_{19} - y_{19}) \mathbf{a}_2 - (z_{19} - \frac{1}{2}) \mathbf{a}_3$	$= -(ax_{19} + c(z_{19} - \frac{1}{2}) \cos \beta) \hat{\mathbf{x}} + by_{19} \hat{\mathbf{y}} -$ $c(z_{19} - \frac{1}{2}) \sin \beta \hat{\mathbf{z}}$	(8f)	Si I
\mathbf{B}_{63}	$-(x_{19} - y_{19}) \mathbf{a}_1 -$ $(x_{19} + y_{19}) \mathbf{a}_2 - z_{19} \mathbf{a}_3$	$= -(ax_{19} + cz_{19} \cos \beta) \hat{\mathbf{x}} - by_{19} \hat{\mathbf{y}} -$ $cz_{19} \sin \beta \hat{\mathbf{z}}$	(8f)	Si I
\mathbf{B}_{64}	$(x_{19} + y_{19}) \mathbf{a}_1 +$ $(x_{19} - y_{19}) \mathbf{a}_2 + (z_{19} + \frac{1}{2}) \mathbf{a}_3$	$= (ax_{19} + c(z_{19} + \frac{1}{2}) \cos \beta) \hat{\mathbf{x}} - by_{19} \hat{\mathbf{y}} +$ $c(z_{19} + \frac{1}{2}) \sin \beta \hat{\mathbf{z}}$	(8f)	Si I
\mathbf{B}_{65}	$(x_{20} - y_{20}) \mathbf{a}_1 +$ $(x_{20} + y_{20}) \mathbf{a}_2 + z_{20} \mathbf{a}_3$	$= (ax_{20} + cz_{20} \cos \beta) \hat{\mathbf{x}} + by_{20} \hat{\mathbf{y}} + cz_{20} \sin \beta \hat{\mathbf{z}}$	(8f)	Si II
\mathbf{B}_{66}	$-(x_{20} + y_{20}) \mathbf{a}_1 -$ $(x_{20} - y_{20}) \mathbf{a}_2 - (z_{20} - \frac{1}{2}) \mathbf{a}_3$	$= -(ax_{20} + c(z_{20} - \frac{1}{2}) \cos \beta) \hat{\mathbf{x}} + by_{20} \hat{\mathbf{y}} -$ $c(z_{20} - \frac{1}{2}) \sin \beta \hat{\mathbf{z}}$	(8f)	Si II
\mathbf{B}_{67}	$-(x_{20} - y_{20}) \mathbf{a}_1 -$ $(x_{20} + y_{20}) \mathbf{a}_2 - z_{20} \mathbf{a}_3$	$= -(ax_{20} + cz_{20} \cos \beta) \hat{\mathbf{x}} - by_{20} \hat{\mathbf{y}} -$ $cz_{20} \sin \beta \hat{\mathbf{z}}$	(8f)	Si II
\mathbf{B}_{68}	$(x_{20} + y_{20}) \mathbf{a}_1 +$ $(x_{20} - y_{20}) \mathbf{a}_2 + (z_{20} + \frac{1}{2}) \mathbf{a}_3$	$= (ax_{20} + c(z_{20} + \frac{1}{2}) \cos \beta) \hat{\mathbf{x}} - by_{20} \hat{\mathbf{y}} +$ $c(z_{20} + \frac{1}{2}) \sin \beta \hat{\mathbf{z}}$	(8f)	Si II
\mathbf{B}_{69}	$(x_{21} - y_{21}) \mathbf{a}_1 +$ $(x_{21} + y_{21}) \mathbf{a}_2 + z_{21} \mathbf{a}_3$	$= (ax_{21} + cz_{21} \cos \beta) \hat{\mathbf{x}} + by_{21} \hat{\mathbf{y}} + cz_{21} \sin \beta \hat{\mathbf{z}}$	(8f)	Si III
\mathbf{B}_{70}	$-(x_{21} + y_{21}) \mathbf{a}_1 -$ $(x_{21} - y_{21}) \mathbf{a}_2 - (z_{21} - \frac{1}{2}) \mathbf{a}_3$	$= -(ax_{21} + c(z_{21} - \frac{1}{2}) \cos \beta) \hat{\mathbf{x}} + by_{21} \hat{\mathbf{y}} -$ $c(z_{21} - \frac{1}{2}) \sin \beta \hat{\mathbf{z}}$	(8f)	Si III

$$\mathbf{B}_{71} = \begin{matrix} -(x_{21} - y_{21}) \mathbf{a}_1 - \\ (x_{21} + y_{21}) \mathbf{a}_2 - z_{21} \mathbf{a}_3 \end{matrix} = \begin{matrix} -(ax_{21} + cz_{21} \cos \beta) \hat{\mathbf{x}} - by_{21} \hat{\mathbf{y}} - \\ cz_{21} \sin \beta \hat{\mathbf{z}} \end{matrix} \quad (8f) \quad \text{Si III}$$

$$\mathbf{B}_{72} = \begin{matrix} (x_{21} + y_{21}) \mathbf{a}_1 + \\ (x_{21} - y_{21}) \mathbf{a}_2 + (z_{21} + \frac{1}{2}) \mathbf{a}_3 \end{matrix} = \begin{matrix} (ax_{21} + c(z_{21} + \frac{1}{2}) \cos \beta) \hat{\mathbf{x}} - by_{21} \hat{\mathbf{y}} + \\ c(z_{21} + \frac{1}{2}) \sin \beta \hat{\mathbf{z}} \end{matrix} \quad (8f) \quad \text{Si III}$$

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