

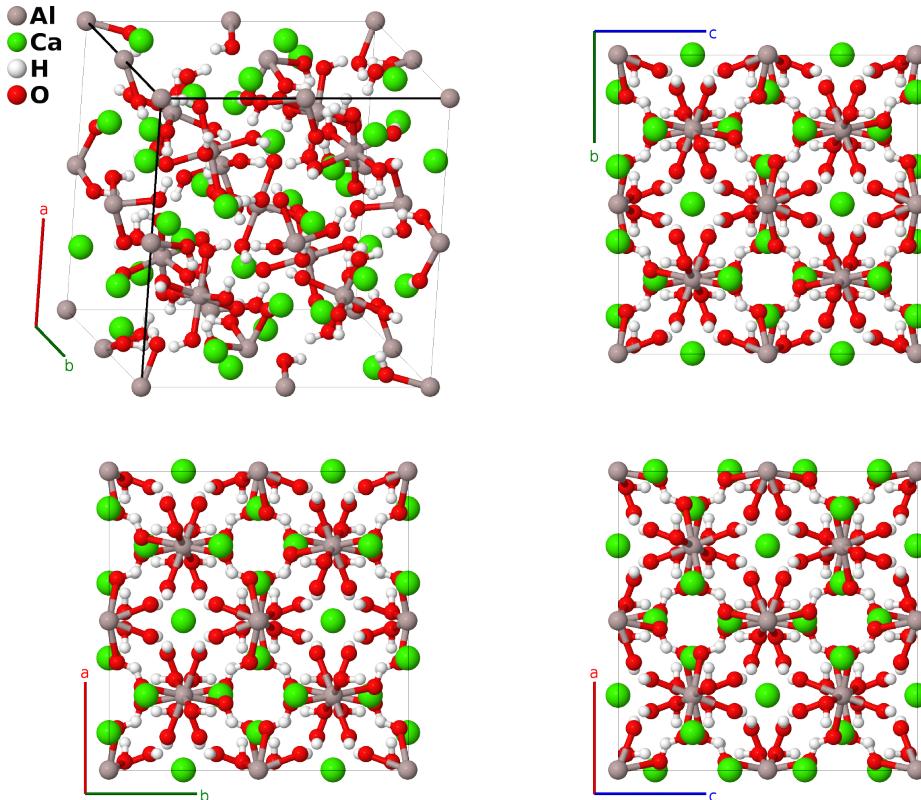
$\text{Ca}_3\text{Al}_2(\text{OH})_{12}$ (J_{23}) Structure: A2B3C12D12_cI232_230_a_c_h_h-001

This structure originally had the label A2B3C12D12_cI232_230_a_c_h_h. Calls to that address will be redirected here.

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<https://aflow.org/p/LL0W>

https://aflow.org/p/A2B3C12D12_cI232_230_a_c_h_h-001

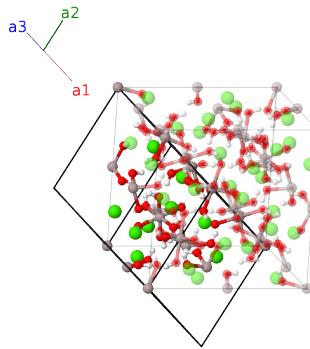


Prototype	$\text{Al}_2\text{Ca}_3\text{H}_{12}\text{O}_{12}$
AFLOW prototype label	A2B3C12D12_cI232_230_a_c_h_h-001
Strukturbericht designation	J_{23}
ICSD	62704
Pearson symbol	cI232
Space group number	230
Space group symbol	$Ia\bar{3}d$
AFLOW prototype command	<pre>aflow --proto=A2B3C12D12_cI232_230_a_c_h_h-001 --params=a,x3,y3,z3,x4,y4,z4</pre>

- The original determination of this structure by (Brandenberger, 1933) did not locate the hydrogen atoms, and according to (Gottfried, 1937) used the coordinates of garnet, $S1_4$. (Bartl, 1986) was able to locate the hydrogen atoms, and as they do not change the space group we include them in the $J2_3$ structure.

Body-centered Cubic primitive vectors

$$\begin{aligned}\mathbf{a}_1 &= -\frac{1}{2}a\hat{\mathbf{x}} + \frac{1}{2}a\hat{\mathbf{y}} + \frac{1}{2}a\hat{\mathbf{z}} \\ \mathbf{a}_2 &= \frac{1}{2}a\hat{\mathbf{x}} - \frac{1}{2}a\hat{\mathbf{y}} + \frac{1}{2}a\hat{\mathbf{z}} \\ \mathbf{a}_3 &= \frac{1}{2}a\hat{\mathbf{x}} + \frac{1}{2}a\hat{\mathbf{y}} - \frac{1}{2}a\hat{\mathbf{z}}\end{aligned}$$



Basis vectors

	Lattice coordinates	=	Cartesian coordinates	Wyckoff position	Atom type
\mathbf{B}_1	0	=	0	(16a)	Al I
\mathbf{B}_2	$\frac{1}{2}\mathbf{a}_1 + \frac{1}{2}\mathbf{a}_3$	=	$\frac{1}{2}a\hat{\mathbf{y}}$	(16a)	Al I
\mathbf{B}_3	$\frac{1}{2}\mathbf{a}_2 + \frac{1}{2}\mathbf{a}_3$	=	$\frac{1}{2}a\hat{\mathbf{x}}$	(16a)	Al I
\mathbf{B}_4	$\frac{1}{2}\mathbf{a}_1 + \frac{1}{2}\mathbf{a}_2$	=	$\frac{1}{2}a\hat{\mathbf{z}}$	(16a)	Al I
\mathbf{B}_5	$\frac{1}{2}\mathbf{a}_1$	=	$-\frac{1}{4}a\hat{\mathbf{x}} + \frac{1}{4}a\hat{\mathbf{y}} + \frac{1}{4}a\hat{\mathbf{z}}$	(16a)	Al I
\mathbf{B}_6	$\frac{1}{2}\mathbf{a}_1 + \frac{1}{2}\mathbf{a}_2 + \frac{1}{2}\mathbf{a}_3$	=	$\frac{1}{4}a\hat{\mathbf{x}} + \frac{1}{4}a\hat{\mathbf{y}} + \frac{1}{4}a\hat{\mathbf{z}}$	(16a)	Al I
\mathbf{B}_7	$\frac{1}{2}\mathbf{a}_3$	=	$\frac{1}{4}a\hat{\mathbf{x}} + \frac{1}{4}a\hat{\mathbf{y}} - \frac{1}{4}a\hat{\mathbf{z}}$	(16a)	Al I
\mathbf{B}_8	$\frac{1}{2}\mathbf{a}_2$	=	$\frac{1}{4}a\hat{\mathbf{x}} - \frac{1}{4}a\hat{\mathbf{y}} + \frac{1}{4}a\hat{\mathbf{z}}$	(16a)	Al I
\mathbf{B}_9	$\frac{1}{4}\mathbf{a}_1 + \frac{3}{8}\mathbf{a}_2 + \frac{1}{8}\mathbf{a}_3$	=	$\frac{1}{8}a\hat{\mathbf{x}} + \frac{1}{4}a\hat{\mathbf{z}}$	(24c)	Ca I
\mathbf{B}_{10}	$\frac{3}{4}\mathbf{a}_1 + \frac{1}{8}\mathbf{a}_2 + \frac{3}{8}\mathbf{a}_3$	=	$-\frac{1}{8}a\hat{\mathbf{x}} + \frac{1}{2}a\hat{\mathbf{y}} + \frac{1}{4}a\hat{\mathbf{z}}$	(24c)	Ca I
\mathbf{B}_{11}	$\frac{1}{8}\mathbf{a}_1 + \frac{1}{4}\mathbf{a}_2 + \frac{3}{8}\mathbf{a}_3$	=	$\frac{1}{4}a\hat{\mathbf{x}} + \frac{1}{8}a\hat{\mathbf{y}}$	(24c)	Ca I
\mathbf{B}_{12}	$\frac{3}{8}\mathbf{a}_1 + \frac{3}{4}\mathbf{a}_2 + \frac{1}{8}\mathbf{a}_3$	=	$\frac{1}{4}a\hat{\mathbf{x}} - \frac{1}{8}a\hat{\mathbf{y}} + \frac{1}{2}a\hat{\mathbf{z}}$	(24c)	Ca I
\mathbf{B}_{13}	$\frac{3}{8}\mathbf{a}_1 + \frac{1}{8}\mathbf{a}_2 + \frac{1}{4}\mathbf{a}_3$	=	$\frac{1}{4}a\hat{\mathbf{y}} + \frac{1}{8}a\hat{\mathbf{z}}$	(24c)	Ca I
\mathbf{B}_{14}	$\frac{1}{8}\mathbf{a}_1 + \frac{3}{8}\mathbf{a}_2 + \frac{3}{4}\mathbf{a}_3$	=	$\frac{1}{2}a\hat{\mathbf{x}} + \frac{1}{4}a\hat{\mathbf{y}} - \frac{1}{8}a\hat{\mathbf{z}}$	(24c)	Ca I
\mathbf{B}_{15}	$\frac{3}{4}\mathbf{a}_1 + \frac{5}{8}\mathbf{a}_2 + \frac{7}{8}\mathbf{a}_3$	=	$\frac{3}{8}a\hat{\mathbf{x}} + \frac{1}{2}a\hat{\mathbf{y}} + \frac{1}{4}a\hat{\mathbf{z}}$	(24c)	Ca I
\mathbf{B}_{16}	$\frac{1}{4}\mathbf{a}_1 + \frac{7}{8}\mathbf{a}_2 + \frac{5}{8}\mathbf{a}_3$	=	$\frac{5}{8}a\hat{\mathbf{x}} + \frac{1}{4}a\hat{\mathbf{z}}$	(24c)	Ca I
\mathbf{B}_{17}	$\frac{7}{8}\mathbf{a}_1 + \frac{3}{4}\mathbf{a}_2 + \frac{5}{8}\mathbf{a}_3$	=	$\frac{1}{4}a\hat{\mathbf{x}} + \frac{3}{8}a\hat{\mathbf{y}} + \frac{1}{2}a\hat{\mathbf{z}}$	(24c)	Ca I
\mathbf{B}_{18}	$\frac{5}{8}\mathbf{a}_1 + \frac{1}{4}\mathbf{a}_2 + \frac{7}{8}\mathbf{a}_3$	=	$\frac{1}{4}a\hat{\mathbf{x}} + \frac{5}{8}a\hat{\mathbf{y}}$	(24c)	Ca I
\mathbf{B}_{19}	$\frac{5}{8}\mathbf{a}_1 + \frac{7}{8}\mathbf{a}_2 + \frac{3}{4}\mathbf{a}_3$	=	$\frac{1}{2}a\hat{\mathbf{x}} + \frac{1}{4}a\hat{\mathbf{y}} + \frac{3}{8}a\hat{\mathbf{z}}$	(24c)	Ca I
\mathbf{B}_{20}	$\frac{7}{8}\mathbf{a}_1 + \frac{5}{8}\mathbf{a}_2 + \frac{1}{4}\mathbf{a}_3$	=	$\frac{1}{4}a\hat{\mathbf{y}} + \frac{5}{8}a\hat{\mathbf{z}}$	(24c)	Ca I
\mathbf{B}_{21}	$(y_3 + z_3)\mathbf{a}_1 + (x_3 + z_3)\mathbf{a}_2 + (x_3 + y_3)\mathbf{a}_3$	=	$ax_3\hat{\mathbf{x}} + ay_3\hat{\mathbf{y}} + az_3\hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{22}	$(-y_3 + z_3 + \frac{1}{2})\mathbf{a}_1 - (x_3 - z_3)\mathbf{a}_2 - (x_3 + y_3 - \frac{1}{2})\mathbf{a}_3$	=	$-ax_3\hat{\mathbf{x}} - a(y_3 - \frac{1}{2})\hat{\mathbf{y}} + az_3\hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{23}	$(y_3 - z_3)\mathbf{a}_1 - (x_3 + z_3 - \frac{1}{2})\mathbf{a}_2 - (-x_3 + y_3 + \frac{1}{2})\mathbf{a}_3$	=	$-a(x_3 - \frac{1}{2})\hat{\mathbf{x}} + ay_3\hat{\mathbf{y}} - az_3\hat{\mathbf{z}}$	(96h)	H I

\mathbf{B}_{24}	$=$	$-\left(y_3 + z_3 - \frac{1}{2}\right) \mathbf{a}_1 +$ $(x_3 - z_3 + \frac{1}{2}) \mathbf{a}_2 + (x_3 - y_3) \mathbf{a}_3$	$=$	$ax_3 \hat{\mathbf{x}} - ay_3 \hat{\mathbf{y}} - a\left(z_3 - \frac{1}{2}\right) \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{25}	$=$	$(x_3 + y_3) \mathbf{a}_1 + (y_3 + z_3) \mathbf{a}_2 +$ $(x_3 + z_3) \mathbf{a}_3$	$=$	$az_3 \hat{\mathbf{x}} + ax_3 \hat{\mathbf{y}} + ay_3 \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{26}	$=$	$-\left(x_3 + y_3 - \frac{1}{2}\right) \mathbf{a}_1 +$ $(-y_3 + z_3 + \frac{1}{2}) \mathbf{a}_2 - (x_3 - z_3) \mathbf{a}_3$	$=$	$az_3 \hat{\mathbf{x}} - ax_3 \hat{\mathbf{y}} - a\left(y_3 - \frac{1}{2}\right) \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{27}	$=$	$(-x_3 + y_3 + \frac{1}{2}) \mathbf{a}_1 +$ $(y_3 - z_3) \mathbf{a}_2 - (x_3 + z_3 - \frac{1}{2}) \mathbf{a}_3$	$=$	$-az_3 \hat{\mathbf{x}} - a\left(x_3 - \frac{1}{2}\right) \hat{\mathbf{y}} + ay_3 \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{28}	$=$	$(x_3 - y_3) \mathbf{a}_1 - (y_3 + z_3 - \frac{1}{2}) \mathbf{a}_2 +$ $(x_3 - z_3 + \frac{1}{2}) \mathbf{a}_3$	$=$	$-a\left(z_3 - \frac{1}{2}\right) \hat{\mathbf{x}} + ax_3 \hat{\mathbf{y}} - ay_3 \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{29}	$=$	$(x_3 + z_3) \mathbf{a}_1 + (x_3 + y_3) \mathbf{a}_2 +$ $(y_3 + z_3) \mathbf{a}_3$	$=$	$ay_3 \hat{\mathbf{x}} + az_3 \hat{\mathbf{y}} + ax_3 \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{30}	$=$	$-(x_3 - z_3) \mathbf{a}_1 -$ $(x_3 + y_3 - \frac{1}{2}) \mathbf{a}_2 +$ $(-y_3 + z_3 + \frac{1}{2}) \mathbf{a}_3$	$=$	$-a\left(y_3 - \frac{1}{2}\right) \hat{\mathbf{x}} + az_3 \hat{\mathbf{y}} - ax_3 \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{31}	$=$	$-\left(x_3 + z_3 - \frac{1}{2}\right) \mathbf{a}_1 +$ $(-x_3 + y_3 + \frac{1}{2}) \mathbf{a}_2 + (y_3 - z_3) \mathbf{a}_3$	$=$	$ay_3 \hat{\mathbf{x}} - az_3 \hat{\mathbf{y}} - a\left(x_3 - \frac{1}{2}\right) \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{32}	$=$	$(x_3 - z_3 + \frac{1}{2}) \mathbf{a}_1 +$ $(x_3 - y_3) \mathbf{a}_2 - (y_3 + z_3 - \frac{1}{2}) \mathbf{a}_3$	$=$	$-ay_3 \hat{\mathbf{x}} - a\left(z_3 - \frac{1}{2}\right) \hat{\mathbf{y}} + ax_3 \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{33}	$=$	$(x_3 - z_3 + \frac{1}{2}) \mathbf{a}_1 +$ $(y_3 - z_3) \mathbf{a}_2 + (x_3 + y_3) \mathbf{a}_3$	$=$	$a\left(y_3 - \frac{1}{4}\right) \hat{\mathbf{x}} + a\left(x_3 + \frac{1}{4}\right) \hat{\mathbf{y}} - a\left(z_3 - \frac{1}{4}\right) \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{34}	$=$	$-(x_3 + z_3 - \frac{1}{2}) \mathbf{a}_1 -$ $(y_3 + z_3 - \frac{1}{2}) \mathbf{a}_2 -$ $(x_3 + y_3 - \frac{1}{2}) \mathbf{a}_3$	$=$	$-a\left(y_3 - \frac{1}{4}\right) \hat{\mathbf{x}} - a\left(x_3 - \frac{1}{4}\right) \hat{\mathbf{y}} - a\left(z_3 - \frac{1}{4}\right) \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{35}	$=$	$-(x_3 - z_3) \mathbf{a}_1 + (y_3 + z_3) \mathbf{a}_2 +$ $(-x_3 + y_3 + \frac{1}{2}) \mathbf{a}_3$	$=$	$a\left(y_3 + \frac{1}{4}\right) \hat{\mathbf{x}} - a\left(x_3 - \frac{1}{4}\right) \hat{\mathbf{y}} + a\left(z_3 - \frac{1}{4}\right) \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{36}	$=$	$(x_3 + z_3) \mathbf{a}_1 +$ $(-y_3 + z_3 + \frac{1}{2}) \mathbf{a}_2 + (x_3 - y_3) \mathbf{a}_3$	$=$	$-a\left(y_3 - \frac{1}{4}\right) \hat{\mathbf{x}} + a\left(x_3 - \frac{1}{4}\right) \hat{\mathbf{y}} + a\left(z_3 + \frac{1}{4}\right) \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{37}	$=$	$(-y_3 + z_3 + \frac{1}{2}) \mathbf{a}_1 +$ $(x_3 - y_3) \mathbf{a}_2 + (x_3 + z_3) \mathbf{a}_3$	$=$	$a\left(x_3 - \frac{1}{4}\right) \hat{\mathbf{x}} + a\left(z_3 + \frac{1}{4}\right) \hat{\mathbf{y}} - a\left(y_3 - \frac{1}{4}\right) \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{38}	$=$	$(y_3 + z_3) \mathbf{a}_1 +$ $(-x_3 + y_3 + \frac{1}{2}) \mathbf{a}_2 - (x_3 - z_3) \mathbf{a}_3$	$=$	$-a\left(x_3 - \frac{1}{4}\right) \hat{\mathbf{x}} + a\left(z_3 - \frac{1}{4}\right) \hat{\mathbf{y}} + a\left(y_3 + \frac{1}{4}\right) \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{39}	$=$	$-(y_3 + z_3 - \frac{1}{2}) \mathbf{a}_1 -$ $(x_3 + y_3 - \frac{1}{2}) \mathbf{a}_2 -$ $(x_3 + z_3 - \frac{1}{2}) \mathbf{a}_3$	$=$	$-a\left(x_3 - \frac{1}{4}\right) \hat{\mathbf{x}} - a\left(z_3 - \frac{1}{4}\right) \hat{\mathbf{y}} - a\left(y_3 - \frac{1}{4}\right) \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{40}	$=$	$(y_3 - z_3) \mathbf{a}_1 + (x_3 + y_3) \mathbf{a}_2 +$ $(x_3 - z_3 + \frac{1}{2}) \mathbf{a}_3$	$=$	$a\left(x_3 + \frac{1}{4}\right) \hat{\mathbf{x}} - a\left(z_3 - \frac{1}{4}\right) \hat{\mathbf{y}} + a\left(y_3 - \frac{1}{4}\right) \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{41}	$=$	$(-x_3 + y_3 + \frac{1}{2}) \mathbf{a}_1 -$ $(x_3 - z_3) \mathbf{a}_2 + (y_3 + z_3) \mathbf{a}_3$	$=$	$a\left(z_3 - \frac{1}{4}\right) \hat{\mathbf{x}} + a\left(y_3 + \frac{1}{4}\right) \hat{\mathbf{y}} - a\left(x_3 - \frac{1}{4}\right) \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{42}	$=$	$(x_3 - y_3) \mathbf{a}_1 + (x_3 + z_3) \mathbf{a}_2 +$ $(-y_3 + z_3 + \frac{1}{2}) \mathbf{a}_3$	$=$	$a\left(z_3 + \frac{1}{4}\right) \hat{\mathbf{x}} - a\left(y_3 - \frac{1}{4}\right) \hat{\mathbf{y}} + a\left(x_3 - \frac{1}{4}\right) \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{43}	$=$	$(x_3 + y_3) \mathbf{a}_1 +$ $(x_3 - z_3 + \frac{1}{2}) \mathbf{a}_2 + (y_3 - z_3) \mathbf{a}_3$	$=$	$-a\left(z_3 - \frac{1}{4}\right) \hat{\mathbf{x}} + a\left(y_3 - \frac{1}{4}\right) \hat{\mathbf{y}} + a\left(x_3 + \frac{1}{4}\right) \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{44}	$=$	$-(x_3 + y_3 - \frac{1}{2}) \mathbf{a}_1 -$ $(x_3 + z_3 - \frac{1}{2}) \mathbf{a}_2 -$ $(y_3 + z_3 - \frac{1}{2}) \mathbf{a}_3$	$=$	$-a\left(z_3 - \frac{1}{4}\right) \hat{\mathbf{x}} - a\left(y_3 - \frac{1}{4}\right) \hat{\mathbf{y}} - a\left(x_3 - \frac{1}{4}\right) \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{45}	$=$	$-(y_3 + z_3) \mathbf{a}_1 - (x_3 + z_3) \mathbf{a}_2 -$ $(x_3 + y_3) \mathbf{a}_3$	$=$	$-ax_3 \hat{\mathbf{x}} - ay_3 \hat{\mathbf{y}} - az_3 \hat{\mathbf{z}}$	(96h)	H I

\mathbf{B}_{46}	$=$	$(y_3 - z_3 + \frac{1}{2}) \mathbf{a}_1 + (x_3 - z_3) \mathbf{a}_2 + (x_3 + y_3 + \frac{1}{2}) \mathbf{a}_3$	$=$	$ax_3 \hat{\mathbf{x}} + a(y_3 + \frac{1}{2}) \hat{\mathbf{y}} - az_3 \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{47}	$=$	$-(y_3 - z_3) \mathbf{a}_1 + (x_3 + z_3 + \frac{1}{2}) \mathbf{a}_2 + (x_3 - y_3 + \frac{1}{2}) \mathbf{a}_3$	$=$	$a(x_3 + \frac{1}{2}) \hat{\mathbf{x}} - ay_3 \hat{\mathbf{y}} + az_3 \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{48}	$=$	$(y_3 + z_3 + \frac{1}{2}) \mathbf{a}_1 + (-x_3 + z_3 + \frac{1}{2}) \mathbf{a}_2 - (x_3 - y_3) \mathbf{a}_3$	$=$	$-ax_3 \hat{\mathbf{x}} + ay_3 \hat{\mathbf{y}} + a(z_3 + \frac{1}{2}) \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{49}	$=$	$-(x_3 + y_3) \mathbf{a}_1 - (y_3 + z_3) \mathbf{a}_2 - (x_3 + z_3) \mathbf{a}_3$	$=$	$-az_3 \hat{\mathbf{x}} - ax_3 \hat{\mathbf{y}} - ay_3 \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{50}	$=$	$(x_3 + y_3 + \frac{1}{2}) \mathbf{a}_1 + (y_3 - z_3 + \frac{1}{2}) \mathbf{a}_2 + (x_3 - z_3) \mathbf{a}_3$	$=$	$-az_3 \hat{\mathbf{x}} + ax_3 \hat{\mathbf{y}} + a(y_3 + \frac{1}{2}) \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{51}	$=$	$(x_3 - y_3 + \frac{1}{2}) \mathbf{a}_1 - (y_3 - z_3) \mathbf{a}_2 + (x_3 + z_3 + \frac{1}{2}) \mathbf{a}_3$	$=$	$az_3 \hat{\mathbf{x}} + a(x_3 + \frac{1}{2}) \hat{\mathbf{y}} - ay_3 \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{52}	$=$	$-(x_3 - y_3) \mathbf{a}_1 + (y_3 + z_3 + \frac{1}{2}) \mathbf{a}_2 + (-x_3 + z_3 + \frac{1}{2}) \mathbf{a}_3$	$=$	$a(z_3 + \frac{1}{2}) \hat{\mathbf{x}} - ax_3 \hat{\mathbf{y}} + ay_3 \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{53}	$=$	$-(x_3 + z_3) \mathbf{a}_1 - (x_3 + y_3) \mathbf{a}_2 - (y_3 + z_3) \mathbf{a}_3$	$=$	$-ay_3 \hat{\mathbf{x}} - az_3 \hat{\mathbf{y}} - ax_3 \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{54}	$=$	$(x_3 - z_3) \mathbf{a}_1 + (x_3 + y_3 + \frac{1}{2}) \mathbf{a}_2 + (y_3 - z_3 + \frac{1}{2}) \mathbf{a}_3$	$=$	$a(y_3 + \frac{1}{2}) \hat{\mathbf{x}} - az_3 \hat{\mathbf{y}} + ax_3 \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{55}	$=$	$(x_3 + z_3 + \frac{1}{2}) \mathbf{a}_1 + (x_3 - y_3 + \frac{1}{2}) \mathbf{a}_2 - (y_3 - z_3) \mathbf{a}_3$	$=$	$-ay_3 \hat{\mathbf{x}} + az_3 \hat{\mathbf{y}} + a(x_3 + \frac{1}{2}) \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{56}	$=$	$(-x_3 + z_3 + \frac{1}{2}) \mathbf{a}_1 - (x_3 - y_3) \mathbf{a}_2 + (y_3 + z_3 + \frac{1}{2}) \mathbf{a}_3$	$=$	$ay_3 \hat{\mathbf{x}} + a(z_3 + \frac{1}{2}) \hat{\mathbf{y}} - ax_3 \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{57}	$=$	$(-x_3 + z_3 + \frac{1}{2}) \mathbf{a}_1 - (y_3 - z_3) \mathbf{a}_2 - (x_3 + y_3) \mathbf{a}_3$	$=$	$-a(y_3 + \frac{1}{4}) \hat{\mathbf{x}} - a(x_3 - \frac{1}{4}) \hat{\mathbf{y}} + a(z_3 + \frac{1}{4}) \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{58}	$=$	$(x_3 + z_3 + \frac{1}{2}) \mathbf{a}_1 + (y_3 + z_3 + \frac{1}{2}) \mathbf{a}_2 + (x_3 + y_3 + \frac{1}{2}) \mathbf{a}_3$	$=$	$a(y_3 + \frac{1}{4}) \hat{\mathbf{x}} + a(x_3 + \frac{1}{4}) \hat{\mathbf{y}} + a(z_3 + \frac{1}{4}) \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{59}	$=$	$(x_3 - z_3) \mathbf{a}_1 - (y_3 + z_3) \mathbf{a}_2 + (x_3 - y_3 + \frac{1}{2}) \mathbf{a}_3$	$=$	$-a(y_3 - \frac{1}{4}) \hat{\mathbf{x}} + a(x_3 + \frac{1}{4}) \hat{\mathbf{y}} - a(z_3 + \frac{1}{4}) \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{60}	$=$	$-(x_3 + z_3) \mathbf{a}_1 + (y_3 - z_3 + \frac{1}{2}) \mathbf{a}_2 - (x_3 - y_3) \mathbf{a}_3$	$=$	$a(y_3 + \frac{1}{4}) \hat{\mathbf{x}} - a(x_3 + \frac{1}{4}) \hat{\mathbf{y}} - a(z_3 - \frac{1}{4}) \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{61}	$=$	$(y_3 - z_3 + \frac{1}{2}) \mathbf{a}_1 - (x_3 - y_3) \mathbf{a}_2 - (x_3 + z_3) \mathbf{a}_3$	$=$	$-a(x_3 + \frac{1}{4}) \hat{\mathbf{x}} - a(z_3 - \frac{1}{4}) \hat{\mathbf{y}} + a(y_3 + \frac{1}{4}) \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{62}	$=$	$-(y_3 + z_3) \mathbf{a}_1 + (x_3 - y_3 + \frac{1}{2}) \mathbf{a}_2 + (x_3 - z_3) \mathbf{a}_3$	$=$	$a(x_3 + \frac{1}{4}) \hat{\mathbf{x}} - a(z_3 + \frac{1}{4}) \hat{\mathbf{y}} - a(y_3 - \frac{1}{4}) \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{63}	$=$	$(y_3 + z_3 + \frac{1}{2}) \mathbf{a}_1 + (x_3 + y_3 + \frac{1}{2}) \mathbf{a}_2 + (x_3 + z_3 + \frac{1}{2}) \mathbf{a}_3$	$=$	$a(x_3 + \frac{1}{4}) \hat{\mathbf{x}} + a(z_3 + \frac{1}{4}) \hat{\mathbf{y}} + a(y_3 + \frac{1}{4}) \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{64}	$=$	$-(y_3 - z_3) \mathbf{a}_1 - (x_3 + y_3) \mathbf{a}_2 + (-x_3 + z_3 + \frac{1}{2}) \mathbf{a}_3$	$=$	$-a(x_3 - \frac{1}{4}) \hat{\mathbf{x}} + a(z_3 + \frac{1}{4}) \hat{\mathbf{y}} - a(y_3 + \frac{1}{4}) \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{65}	$=$	$(x_3 - y_3 + \frac{1}{2}) \mathbf{a}_1 + (x_3 - z_3) \mathbf{a}_2 - (y_3 + z_3) \mathbf{a}_3$	$=$	$-a(z_3 + \frac{1}{4}) \hat{\mathbf{x}} - a(y_3 - \frac{1}{4}) \hat{\mathbf{y}} + a(x_3 + \frac{1}{4}) \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{66}	$=$	$-(x_3 - y_3) \mathbf{a}_1 - (x_3 + z_3) \mathbf{a}_2 + (y_3 - z_3 + \frac{1}{2}) \mathbf{a}_3$	$=$	$-a(z_3 - \frac{1}{4}) \hat{\mathbf{x}} + a(y_3 + \frac{1}{4}) \hat{\mathbf{y}} - a(x_3 + \frac{1}{4}) \hat{\mathbf{z}}$	(96h)	H I
\mathbf{B}_{67}	$=$	$-(x_3 + y_3) \mathbf{a}_1 + (-x_3 + z_3 + \frac{1}{2}) \mathbf{a}_2 - (y_3 - z_3) \mathbf{a}_3$	$=$	$a(z_3 + \frac{1}{4}) \hat{\mathbf{x}} - a(y_3 + \frac{1}{4}) \hat{\mathbf{y}} - a(x_3 - \frac{1}{4}) \hat{\mathbf{z}}$	(96h)	H I

B₆₈	$(x_3 + y_3 + \frac{1}{2}) \mathbf{a}_1 +$ $(x_3 + z_3 + \frac{1}{2}) \mathbf{a}_2 +$ $(y_3 + z_3 + \frac{1}{2}) \mathbf{a}_3$	$= a(z_3 + \frac{1}{4}) \hat{\mathbf{x}} + a(y_3 + \frac{1}{4}) \hat{\mathbf{y}} + a(x_3 + \frac{1}{4}) \hat{\mathbf{z}}$	(96h)	H I
B₆₉	$(y_4 + z_4) \mathbf{a}_1 + (x_4 + z_4) \mathbf{a}_2 +$ $(x_4 + y_4) \mathbf{a}_3$	$= ax_4 \hat{\mathbf{x}} + ay_4 \hat{\mathbf{y}} + az_4 \hat{\mathbf{z}}$	(96h)	O I
B₇₀	$(-y_4 + z_4 + \frac{1}{2}) \mathbf{a}_1 -$ $(x_4 - z_4) \mathbf{a}_2 - (x_4 + y_4 - \frac{1}{2}) \mathbf{a}_3$	$= -ax_4 \hat{\mathbf{x}} - a(y_4 - \frac{1}{2}) \hat{\mathbf{y}} + az_4 \hat{\mathbf{z}}$	(96h)	O I
B₇₁	$(y_4 - z_4) \mathbf{a}_1 - (x_4 + z_4 - \frac{1}{2}) \mathbf{a}_2 +$ $(-x_4 + y_4 + \frac{1}{2}) \mathbf{a}_3$	$= -a(x_4 - \frac{1}{2}) \hat{\mathbf{x}} + ay_4 \hat{\mathbf{y}} - az_4 \hat{\mathbf{z}}$	(96h)	O I
B₇₂	$-(y_4 + z_4 - \frac{1}{2}) \mathbf{a}_1 +$ $(x_4 - z_4 + \frac{1}{2}) \mathbf{a}_2 + (x_4 - y_4) \mathbf{a}_3$	$= ax_4 \hat{\mathbf{x}} - ay_4 \hat{\mathbf{y}} - a(z_4 - \frac{1}{2}) \hat{\mathbf{z}}$	(96h)	O I
B₇₃	$(x_4 + y_4) \mathbf{a}_1 + (y_4 + z_4) \mathbf{a}_2 +$ $(x_4 + z_4) \mathbf{a}_3$	$= az_4 \hat{\mathbf{x}} + ax_4 \hat{\mathbf{y}} + ay_4 \hat{\mathbf{z}}$	(96h)	O I
B₇₄	$-(x_4 + y_4 - \frac{1}{2}) \mathbf{a}_1 +$ $(-y_4 + z_4 + \frac{1}{2}) \mathbf{a}_2 - (x_4 - z_4) \mathbf{a}_3$	$= az_4 \hat{\mathbf{x}} - ax_4 \hat{\mathbf{y}} - a(y_4 - \frac{1}{2}) \hat{\mathbf{z}}$	(96h)	O I
B₇₅	$(-x_4 + y_4 + \frac{1}{2}) \mathbf{a}_1 +$ $(y_4 - z_4) \mathbf{a}_2 - (x_4 + z_4 - \frac{1}{2}) \mathbf{a}_3$	$= -az_4 \hat{\mathbf{x}} - a(x_4 - \frac{1}{2}) \hat{\mathbf{y}} + ay_4 \hat{\mathbf{z}}$	(96h)	O I
B₇₆	$(x_4 - y_4) \mathbf{a}_1 - (y_4 + z_4 - \frac{1}{2}) \mathbf{a}_2 +$ $(x_4 - z_4 + \frac{1}{2}) \mathbf{a}_3$	$= -a(z_4 - \frac{1}{2}) \hat{\mathbf{x}} + ax_4 \hat{\mathbf{y}} - ay_4 \hat{\mathbf{z}}$	(96h)	O I
B₇₇	$(x_4 + z_4) \mathbf{a}_1 + (x_4 + y_4) \mathbf{a}_2 +$ $(y_4 + z_4) \mathbf{a}_3$	$= ay_4 \hat{\mathbf{x}} + az_4 \hat{\mathbf{y}} + ax_4 \hat{\mathbf{z}}$	(96h)	O I
B₇₈	$-(x_4 - z_4) \mathbf{a}_1 -$ $(x_4 + y_4 - \frac{1}{2}) \mathbf{a}_2 +$ $(-y_4 + z_4 + \frac{1}{2}) \mathbf{a}_3$	$= -a(y_4 - \frac{1}{2}) \hat{\mathbf{x}} + az_4 \hat{\mathbf{y}} - ax_4 \hat{\mathbf{z}}$	(96h)	O I
B₇₉	$-(x_4 + z_4 - \frac{1}{2}) \mathbf{a}_1 +$ $(-x_4 + y_4 + \frac{1}{2}) \mathbf{a}_2 + (y_4 - z_4) \mathbf{a}_3$	$= ay_4 \hat{\mathbf{x}} - az_4 \hat{\mathbf{y}} - a(x_4 - \frac{1}{2}) \hat{\mathbf{z}}$	(96h)	O I
B₈₀	$(x_4 - z_4 + \frac{1}{2}) \mathbf{a}_1 +$ $(x_4 - y_4) \mathbf{a}_2 - (y_4 + z_4 - \frac{1}{2}) \mathbf{a}_3$	$= -ay_4 \hat{\mathbf{x}} - a(z_4 - \frac{1}{2}) \hat{\mathbf{y}} + ax_4 \hat{\mathbf{z}}$	(96h)	O I
B₈₁	$(x_4 - z_4 + \frac{1}{2}) \mathbf{a}_1 +$ $(y_4 - z_4) \mathbf{a}_2 + (x_4 + y_4) \mathbf{a}_3$	$= a(y_4 - \frac{1}{4}) \hat{\mathbf{x}} + a(x_4 + \frac{1}{4}) \hat{\mathbf{y}} - a(z_4 - \frac{1}{4}) \hat{\mathbf{z}}$	(96h)	O I
B₈₂	$-(x_4 + z_4 - \frac{1}{2}) \mathbf{a}_1 -$ $(y_4 + z_4 - \frac{1}{2}) \mathbf{a}_2 -$ $(x_4 + y_4 - \frac{1}{2}) \mathbf{a}_3$	$= -a(y_4 - \frac{1}{4}) \hat{\mathbf{x}} - a(x_4 - \frac{1}{4}) \hat{\mathbf{y}} - a(z_4 - \frac{1}{4}) \hat{\mathbf{z}}$	(96h)	O I
B₈₃	$-(x_4 - z_4) \mathbf{a}_1 + (y_4 + z_4) \mathbf{a}_2 +$ $(-x_4 + y_4 + \frac{1}{2}) \mathbf{a}_3$	$= a(y_4 + \frac{1}{4}) \hat{\mathbf{x}} - a(x_4 - \frac{1}{4}) \hat{\mathbf{y}} + a(z_4 - \frac{1}{4}) \hat{\mathbf{z}}$	(96h)	O I
B₈₄	$(x_4 + z_4) \mathbf{a}_1 +$ $(-y_4 + z_4 + \frac{1}{2}) \mathbf{a}_2 + (x_4 - y_4) \mathbf{a}_3$	$= -a(y_4 - \frac{1}{4}) \hat{\mathbf{x}} + a(x_4 - \frac{1}{4}) \hat{\mathbf{y}} + a(z_4 + \frac{1}{4}) \hat{\mathbf{z}}$	(96h)	O I
B₈₅	$(-y_4 + z_4 + \frac{1}{2}) \mathbf{a}_1 +$ $(x_4 - y_4) \mathbf{a}_2 + (x_4 + z_4) \mathbf{a}_3$	$= a(x_4 - \frac{1}{4}) \hat{\mathbf{x}} + a(z_4 + \frac{1}{4}) \hat{\mathbf{y}} - a(y_4 - \frac{1}{4}) \hat{\mathbf{z}}$	(96h)	O I
B₈₆	$(y_4 + z_4) \mathbf{a}_1 +$ $(-x_4 + y_4 + \frac{1}{2}) \mathbf{a}_2 - (x_4 - z_4) \mathbf{a}_3$	$= -a(x_4 - \frac{1}{4}) \hat{\mathbf{x}} + a(z_4 - \frac{1}{4}) \hat{\mathbf{y}} + a(y_4 + \frac{1}{4}) \hat{\mathbf{z}}$	(96h)	O I
B₈₇	$-(y_4 + z_4 - \frac{1}{2}) \mathbf{a}_1 -$ $(x_4 + y_4 - \frac{1}{2}) \mathbf{a}_2 -$ $(x_4 + z_4 - \frac{1}{2}) \mathbf{a}_3$	$= -a(x_4 - \frac{1}{4}) \hat{\mathbf{x}} - a(z_4 - \frac{1}{4}) \hat{\mathbf{y}} - a(y_4 - \frac{1}{4}) \hat{\mathbf{z}}$	(96h)	O I
B₈₈	$(y_4 - z_4) \mathbf{a}_1 + (x_4 + y_4) \mathbf{a}_2 +$ $(x_4 - z_4 + \frac{1}{2}) \mathbf{a}_3$	$= a(x_4 + \frac{1}{4}) \hat{\mathbf{x}} - a(z_4 - \frac{1}{4}) \hat{\mathbf{y}} + a(y_4 - \frac{1}{4}) \hat{\mathbf{z}}$	(96h)	O I
B₈₉	$(-x_4 + y_4 + \frac{1}{2}) \mathbf{a}_1 -$ $(x_4 - z_4) \mathbf{a}_2 + (y_4 + z_4) \mathbf{a}_3$	$= a(z_4 - \frac{1}{4}) \hat{\mathbf{x}} + a(y_4 + \frac{1}{4}) \hat{\mathbf{y}} - a(x_4 - \frac{1}{4}) \hat{\mathbf{z}}$	(96h)	O I

B₉₀	$=$	$(x_4 - y_4) \mathbf{a}_1 + (x_4 + z_4) \mathbf{a}_2 + (-y_4 + z_4 + \frac{1}{2}) \mathbf{a}_3$	$=$	$a(z_4 + \frac{1}{4}) \hat{\mathbf{x}} - a(y_4 - \frac{1}{4}) \hat{\mathbf{y}} + a(x_4 - \frac{1}{4}) \hat{\mathbf{z}}$	(96h)	O I
B₉₁	$=$	$(x_4 + y_4) \mathbf{a}_1 + (x_4 - z_4 + \frac{1}{2}) \mathbf{a}_2 + (y_4 - z_4) \mathbf{a}_3$	$=$	$-a(z_4 - \frac{1}{4}) \hat{\mathbf{x}} + a(y_4 - \frac{1}{4}) \hat{\mathbf{y}} + a(x_4 + \frac{1}{4}) \hat{\mathbf{z}}$	(96h)	O I
B₉₂	$=$	$-(x_4 + y_4 - \frac{1}{2}) \mathbf{a}_1 - (x_4 + z_4 - \frac{1}{2}) \mathbf{a}_2 - (y_4 + z_4 - \frac{1}{2}) \mathbf{a}_3$	$=$	$-a(z_4 - \frac{1}{4}) \hat{\mathbf{x}} - a(y_4 - \frac{1}{4}) \hat{\mathbf{y}} - a(x_4 - \frac{1}{4}) \hat{\mathbf{z}}$	(96h)	O I
B₉₃	$=$	$-(y_4 + z_4) \mathbf{a}_1 - (x_4 + z_4) \mathbf{a}_2 - (x_4 + y_4) \mathbf{a}_3$	$=$	$-ax_4 \hat{\mathbf{x}} - ay_4 \hat{\mathbf{y}} - az_4 \hat{\mathbf{z}}$	(96h)	O I
B₉₄	$=$	$(y_4 - z_4 + \frac{1}{2}) \mathbf{a}_1 + (x_4 - z_4) \mathbf{a}_2 + (x_4 + y_4 + \frac{1}{2}) \mathbf{a}_3$	$=$	$ax_4 \hat{\mathbf{x}} + a(y_4 + \frac{1}{2}) \hat{\mathbf{y}} - az_4 \hat{\mathbf{z}}$	(96h)	O I
B₉₅	$=$	$-(y_4 - z_4) \mathbf{a}_1 + (x_4 + z_4 + \frac{1}{2}) \mathbf{a}_2 + (x_4 - y_4 + \frac{1}{2}) \mathbf{a}_3$	$=$	$a(x_4 + \frac{1}{2}) \hat{\mathbf{x}} - ay_4 \hat{\mathbf{y}} + az_4 \hat{\mathbf{z}}$	(96h)	O I
B₉₆	$=$	$(y_4 + z_4 + \frac{1}{2}) \mathbf{a}_1 + (-x_4 + z_4 + \frac{1}{2}) \mathbf{a}_2 - (x_4 - y_4) \mathbf{a}_3$	$=$	$-ax_4 \hat{\mathbf{x}} + ay_4 \hat{\mathbf{y}} + a(z_4 + \frac{1}{2}) \hat{\mathbf{z}}$	(96h)	O I
B₉₇	$=$	$-(x_4 + y_4) \mathbf{a}_1 - (y_4 + z_4) \mathbf{a}_2 - (x_4 + z_4) \mathbf{a}_3$	$=$	$-az_4 \hat{\mathbf{x}} - ax_4 \hat{\mathbf{y}} - ay_4 \hat{\mathbf{z}}$	(96h)	O I
B₉₈	$=$	$(x_4 + y_4 + \frac{1}{2}) \mathbf{a}_1 + (y_4 - z_4 + \frac{1}{2}) \mathbf{a}_2 + (x_4 - z_4) \mathbf{a}_3$	$=$	$-az_4 \hat{\mathbf{x}} + ax_4 \hat{\mathbf{y}} + a(y_4 + \frac{1}{2}) \hat{\mathbf{z}}$	(96h)	O I
B₉₉	$=$	$(x_4 - y_4 + \frac{1}{2}) \mathbf{a}_1 - (y_4 - z_4) \mathbf{a}_2 + (x_4 + z_4 + \frac{1}{2}) \mathbf{a}_3$	$=$	$az_4 \hat{\mathbf{x}} + a(x_4 + \frac{1}{2}) \hat{\mathbf{y}} - ay_4 \hat{\mathbf{z}}$	(96h)	O I
B₁₀₀	$=$	$-(x_4 - y_4) \mathbf{a}_1 + (y_4 + z_4 + \frac{1}{2}) \mathbf{a}_2 + (-x_4 + z_4 + \frac{1}{2}) \mathbf{a}_3$	$=$	$a(z_4 + \frac{1}{2}) \hat{\mathbf{x}} - ax_4 \hat{\mathbf{y}} + ay_4 \hat{\mathbf{z}}$	(96h)	O I
B₁₀₁	$=$	$-(x_4 + z_4) \mathbf{a}_1 - (x_4 + y_4) \mathbf{a}_2 - (y_4 + z_4) \mathbf{a}_3$	$=$	$-ay_4 \hat{\mathbf{x}} - az_4 \hat{\mathbf{y}} - ax_4 \hat{\mathbf{z}}$	(96h)	O I
B₁₀₂	$=$	$(x_4 - z_4) \mathbf{a}_1 + (x_4 + y_4 + \frac{1}{2}) \mathbf{a}_2 + (y_4 - z_4 + \frac{1}{2}) \mathbf{a}_3$	$=$	$a(y_4 + \frac{1}{2}) \hat{\mathbf{x}} - az_4 \hat{\mathbf{y}} + ax_4 \hat{\mathbf{z}}$	(96h)	O I
B₁₀₃	$=$	$(x_4 + z_4 + \frac{1}{2}) \mathbf{a}_1 + (x_4 - y_4 + \frac{1}{2}) \mathbf{a}_2 - (y_4 - z_4) \mathbf{a}_3$	$=$	$-ay_4 \hat{\mathbf{x}} + az_4 \hat{\mathbf{y}} + a(x_4 + \frac{1}{2}) \hat{\mathbf{z}}$	(96h)	O I
B₁₀₄	$=$	$(-x_4 + z_4 + \frac{1}{2}) \mathbf{a}_1 - (x_4 - y_4) \mathbf{a}_2 + (y_4 + z_4 + \frac{1}{2}) \mathbf{a}_3$	$=$	$ay_4 \hat{\mathbf{x}} + a(z_4 + \frac{1}{2}) \hat{\mathbf{y}} - ax_4 \hat{\mathbf{z}}$	(96h)	O I
B₁₀₅	$=$	$(-x_4 + z_4 + \frac{1}{2}) \mathbf{a}_1 - (y_4 - z_4) \mathbf{a}_2 - (x_4 + y_4) \mathbf{a}_3$	$=$	$-a(y_4 + \frac{1}{4}) \hat{\mathbf{x}} - a(x_4 - \frac{1}{4}) \hat{\mathbf{y}} + a(z_4 + \frac{1}{4}) \hat{\mathbf{z}}$	(96h)	O I
B₁₀₆	$=$	$(x_4 + z_4 + \frac{1}{2}) \mathbf{a}_1 + (y_4 + z_4 + \frac{1}{2}) \mathbf{a}_2 + (x_4 + y_4 + \frac{1}{2}) \mathbf{a}_3$	$=$	$a(y_4 + \frac{1}{4}) \hat{\mathbf{x}} + a(x_4 + \frac{1}{4}) \hat{\mathbf{y}} + a(z_4 + \frac{1}{4}) \hat{\mathbf{z}}$	(96h)	O I
B₁₀₇	$=$	$(x_4 - z_4) \mathbf{a}_1 - (y_4 + z_4) \mathbf{a}_2 + (x_4 - y_4 + \frac{1}{2}) \mathbf{a}_3$	$=$	$-a(y_4 - \frac{1}{4}) \hat{\mathbf{x}} + a(x_4 + \frac{1}{4}) \hat{\mathbf{y}} - a(z_4 + \frac{1}{4}) \hat{\mathbf{z}}$	(96h)	O I
B₁₀₈	$=$	$-(x_4 + z_4) \mathbf{a}_1 + (y_4 - z_4 + \frac{1}{2}) \mathbf{a}_2 - (x_4 - y_4) \mathbf{a}_3$	$=$	$a(y_4 + \frac{1}{4}) \hat{\mathbf{x}} - a(x_4 + \frac{1}{4}) \hat{\mathbf{y}} - a(z_4 - \frac{1}{4}) \hat{\mathbf{z}}$	(96h)	O I
B₁₀₉	$=$	$(y_4 - z_4 + \frac{1}{2}) \mathbf{a}_1 - (x_4 - y_4) \mathbf{a}_2 - (x_4 + z_4) \mathbf{a}_3$	$=$	$-a(x_4 + \frac{1}{4}) \hat{\mathbf{x}} - a(z_4 - \frac{1}{4}) \hat{\mathbf{y}} + a(y_4 + \frac{1}{4}) \hat{\mathbf{z}}$	(96h)	O I
B₁₁₀	$=$	$-(y_4 + z_4) \mathbf{a}_1 + (x_4 - y_4 + \frac{1}{2}) \mathbf{a}_2 + (x_4 - z_4) \mathbf{a}_3$	$=$	$a(x_4 + \frac{1}{4}) \hat{\mathbf{x}} - a(z_4 + \frac{1}{4}) \hat{\mathbf{y}} - a(y_4 - \frac{1}{4}) \hat{\mathbf{z}}$	(96h)	O I

$$\begin{aligned}
\mathbf{B}_{111} &= \left(y_4 + z_4 + \frac{1}{2} \right) \mathbf{a}_1 + \left(x_4 + y_4 + \frac{1}{2} \right) \mathbf{a}_2 + \left(x_4 + z_4 + \frac{1}{2} \right) \mathbf{a}_3 & = a \left(x_4 + \frac{1}{4} \right) \hat{\mathbf{x}} + a \left(z_4 + \frac{1}{4} \right) \hat{\mathbf{y}} + a \left(y_4 + \frac{1}{4} \right) \hat{\mathbf{z}} & (96h) & O I \\
\mathbf{B}_{112} &= - (y_4 - z_4) \mathbf{a}_1 - (x_4 + y_4) \mathbf{a}_2 + \left(-x_4 + z_4 + \frac{1}{2} \right) \mathbf{a}_3 & = -a \left(x_4 - \frac{1}{4} \right) \hat{\mathbf{x}} + a \left(z_4 + \frac{1}{4} \right) \hat{\mathbf{y}} - a \left(y_4 + \frac{1}{4} \right) \hat{\mathbf{z}} & (96h) & O I \\
\mathbf{B}_{113} &= \left(x_4 - y_4 + \frac{1}{2} \right) \mathbf{a}_1 + \left(x_4 - z_4 \right) \mathbf{a}_2 - \left(y_4 + z_4 \right) \mathbf{a}_3 & = -a \left(z_4 + \frac{1}{4} \right) \hat{\mathbf{x}} - a \left(y_4 - \frac{1}{4} \right) \hat{\mathbf{y}} + a \left(x_4 + \frac{1}{4} \right) \hat{\mathbf{z}} & (96h) & O I \\
\mathbf{B}_{114} &= - (x_4 - y_4) \mathbf{a}_1 - (x_4 + z_4) \mathbf{a}_2 + \left(y_4 - z_4 + \frac{1}{2} \right) \mathbf{a}_3 & = -a \left(z_4 - \frac{1}{4} \right) \hat{\mathbf{x}} + a \left(y_4 + \frac{1}{4} \right) \hat{\mathbf{y}} - a \left(x_4 + \frac{1}{4} \right) \hat{\mathbf{z}} & (96h) & O I \\
\mathbf{B}_{115} &= - (x_4 + y_4) \mathbf{a}_1 + \left(-x_4 + z_4 + \frac{1}{2} \right) \mathbf{a}_2 - \left(y_4 - z_4 \right) \mathbf{a}_3 & = a \left(z_4 + \frac{1}{4} \right) \hat{\mathbf{x}} - a \left(y_4 + \frac{1}{4} \right) \hat{\mathbf{y}} - a \left(x_4 - \frac{1}{4} \right) \hat{\mathbf{z}} & (96h) & O I \\
\mathbf{B}_{116} &= \left(x_4 + y_4 + \frac{1}{2} \right) \mathbf{a}_1 + \left(x_4 + z_4 + \frac{1}{2} \right) \mathbf{a}_2 + \left(y_4 + z_4 + \frac{1}{2} \right) \mathbf{a}_3 & = a \left(z_4 + \frac{1}{4} \right) \hat{\mathbf{x}} + a \left(y_4 + \frac{1}{4} \right) \hat{\mathbf{y}} + a \left(x_4 + \frac{1}{4} \right) \hat{\mathbf{z}} & (96h) & O I
\end{aligned}$$

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